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## Detection of low-energy electrons with transition-edge sensors

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We present the detection of electrons with kinetic energy in the 100 eV range with transition-edge sensors (TESs). This has been achieved with a  $(100 \times 100)$ - $\mu$ m<sup>2</sup> Ti/Au bilayer TES, with a critical temperature of about 84 mK. The electrons are produced directly in the cryostat by an innovative cold source based on field emission from vertically aligned multiwall carbon nanotubes. We obtain a Gaussian energy resolution between 0.8 and 1.8 eV for fully absorbed electrons in the (90–101) eV energy range, which is found to be compatible with the resolution of this same device for photons in the same energy range. This work opens possibilities for high-precision energy measurements of low-energy electrons.

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Transition-edge sensors (TESs) are highly sensitive microcalorimeters capable of high-resolution singlephoton counting across a wide energy spectrum [1,2]. The detection scheme is based on the absorption of photons in a thin superconducting film, in which their energy is transformed into heat. By operating a TES at its critical temperature  $T_{\rm C}$ , even small variations in temperature lead to measurable changes in its electrical resistance, owing to the steep transition between the superconducting regime and the normal-conduction one. TES devices have been capable of achieving single-photon Gaussian energy resolutions below 50 meV for 0.8-eV photons [3,4].

In principle, this detection scheme should also be sensitive to electrons absorbed in the superconducting film. However, there is currently very limited research on TES electron detection, except for a recent result [5] for electrons in the 300–2000 eV energy range, which achieves a Gaussian energy resolution  $\sigma_e > 17$  eV. Low-energy electrons have been detected using various devices, such as microchannel plates [6], which suffer from poor energy resolution and geometrical inefficiencies due to their nonunitary fill factor. Silicon-based detectors, including avalanche photodiodes [7] and silicon drift detectors [8], face challenges such as dead layers at the detector entrance, where low-energy electrons are absorbed before producing a signal.

In contrast, TES devices offer a detection scheme that, in principle, is free of dead layers and features a unitary fill factor, providing the potential for high efficiency and excellent intrinsic energy resolution. These features make this technology potentially very interesting for low-energy electron spectroscopy [5], microcalorimetry [9,10], and for experiments studying  $\beta$ -decay and neutrino physics. One example is the PTOLEMY project, which aims to detect the cosmic neutrino background by analyzing the endpoint of the  $\beta^-$  decay of tritium, seeking to achieve an electron energy resolution of 50 meV for 10-eV electrons [11–13].

In this work, electrons are produced by field emission from vertically aligned carbon nanotubes (CNTs). This innovative cold-source solution overcomes the issues in interfacing standard hot-filament-based electron sources with the TES working at cryogenic temperature, thus allowing the source to be placed directly inside the cryostat, close to the TES.

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The results presented in the following were obtained in the Innovative Cryogenic Detectors Laboratory of Istituto Nazionale di Ricerca Metrologica (INRiM) in Torino (Italy) [14]. The TES detector operates inside an adiabatic demagnetization refrigerator cryostat, at a stable bath temperature  $T_{\text{bath}} = 41.7 \pm 0.2$  mK, as measured by a ruthenium oxide thermal sensor. To suppress magnetic interference affecting the electrons in motion, TESs, and dc SQUIDs (superconducting quantum interference devices), a cryogenic magnetic shield is installed around the working area within the cryostat.

A schematic view of the layers that compose the TES and its surroundings is shown in Fig. 1(a). The TES device used in this work was fabricated at QR Lab, INRiM, has an area of  $(100 \times 100) \,\mu\text{m}^2$ , and is a Ti/Au bilayer device, composed of a 15-nm layer of titanium covered by a 30-nm layer of gold, deposited by thermal evaporation on a silicon substrate covered by 150 nm of  $SiO_2$  and 500 nm of  $SiN_x$ on both sides [15]. The wiring is done with 50-nm superconducting niobium strips, deposited on the substrate via sputtering. The TES has a critical temperature  $T_{\rm C} = 84 \, {\rm mK}$ and is characterized in the (3–140) eV energy range with 406-nm photons from a pulsed laser. By varying the laser intensity, the number of photons per bunch  $N_{\nu}$  can be adjusted. The result of this characterization, in the energy range of interest for this work, is shown in Fig. 2: the peaks corresponding to  $30 \le N_{\gamma} \le 34$  are clearly distinguishable, and fitted with a sum of Gaussian functions. The



FIG. 1. (a) Schematic view of the TES device and its shield layer (y axis to scale, x axis not to scale). (b) Schematic view of the setup. (c) Schematic view of the electrical circuit.



FIG. 2. TES optical characterization with  $\lambda_{\gamma} = 406$ -nm photons. The histogram of the pulse amplitudes reports peaks corresponding to  $30 \le N_{\gamma} \le 34$ , which are clearly distinguishable, and fitted with a sum of Gaussian functions (red line).

dark count of the TES is found to be negligible compared with the signal rate with the trigger threshold used in this work, as expected from this type of device [16].

This TES is adapted for electron detection by adding a shield layer, which is needed as the electron source has a significantly larger area compared with the TES. The shield leaves the TES active area exposed, but covers the area surrounding it, as direct electron hits on the wiring would induce electrical noise, and hits on the insulating substrate would lead to charge build-up. The shield layer is produced by thermal evaporation, depositing an insulating layer consisting of 300 nm of amorphous silicon oxide  $(SiO_x)$  [17], followed by a thin (5-nm) layer of titanium, and finally a 50-nm layer of gold. The titanium layer is necessary for best adhesion of gold to the SiO<sub>x</sub>.

The electron source consists of a sample of vertically aligned multiwall CNTs synthesized in the INFN laboratory "TITAN" at Sapienza University of Rome [18–21]. The nanotubes are grown through chemical vapor deposition on a 500- $\mu$ m silicon substrate, and cover a surface of roughly (3 × 3) mm<sup>2</sup>. Because of the high geometrical field enhancement factor of their tips, nanotubes are capable of emitting electrons through quantum tunneling (field emission) without the necessity of very high voltages [22–25]. Furthermore, field emission does not generate heat and can therefore be used in a cryostat.

The TES and the nanotubes are placed on two copper plates, facing each other, separated by 0.5-mm sapphire spacers, which ensure electrical insulation while guaranteeing a good degree of thermal conductance. The top copper plate, where the nanotubes are hosted, is provided with a negative voltage  $V_{\text{CNT}}$  to induce field emission. The bottom plate is in thermal contact with the cryostat and electrically grounded through it. The distance between the tips of the nanotubes and the surface of the TES is  $d = 600 \pm 50 \,\mu\text{m}$ . A schematic view of the setup is shown in Fig. 1(b).

In field emission electrons tunnel through the potential barrier, and are therefore emitted at a potential  $\phi_{CNT}$  below the vacuum level, where  $\phi_{CNT}$  is the work function of the CNTs [26]. Additionally, the difference between the work functions of the CNTs and the TES will create an effective field that will further correct the kinetic energy of the electrons  $E_e$ . In the form of a formula:

$$E_{\rm e} = eV_{\rm CNT} - \phi_{\rm CNT} + (\phi_{\rm CNT} - \phi_{\rm TES}) = eV_{\rm CNT} - \phi_{\rm TES},$$
(1)

where *e* is the elementary charge. The TES work function is measured with ultraviolet photoemission spectroscopy in Roma Tre University's LASEC lab, obtaining  $\phi_{\text{TES}} =$  $4.38 \pm 0.03$  eV. Moreover, the source is monochromatic, as the energy spread of the field-emitted electrons is negligible with the values of temperature and electric field of our setup [27].

The electron emission from the CNTs is measured in two different ways, as shown in the electrical circuits in Fig. 1(c): by connecting a Keithley 6487 picoammeter to the metallic shield layer, to measure the current  $I_{\text{CNT}}$ ; and by counting the signals in the TES, while operating it at a working point of  $R_0 = 0.35R_N$ , where  $R_N = 246 \text{ m}\Omega$  is the resistance of the TES in its normal state. This working point is found to be optimal in terms of energy resolution during the optical characterization. The TES is operated in electrothermal feedback and read out by a SQUID array [28] coupled to the inductance L = 6 nH.

The  $I_{\rm CNT}$  measurements, as a function of  $V_{\rm CNT}$ , are summarized by the black curve of Fig. 3. As can be seen,  $I_{\rm CNT}$  exhibits an exponential rise, compatible with the Fowler-Nordheim theory on field emission [29]. Superimposed with red markers is the rate of counts recorded by the TES, which follows the same exponential rise as  $I_{\rm CNT}$ , therefore proving that the signals recorded by the TES are due to electrons. The inset in Fig. 3 shows a typical TES signal for  $V_{\rm CNT} = 100$  V, characterized by a rise time  $\tau_+ \approx 200$  ns and a recovery time  $\tau_- \approx 10 \,\mu$ s.

A feature of Fowler-Nordheim emission is that the electron current depends on the electric field  $|\vec{E}|$ , which in our planar configuration is approximated by  $|\vec{E}| = V_{\rm CNT}/d$ . Moreover, the kinetic energy of these electrons is also determined by  $V_{\rm CNT}$ , as shown in Eq. (1). Therefore, in our setup, the signal rate and energy are not independent parameters, as they both depend on  $V_{\rm CNT}$ .



FIG. 3. Current  $I_{\text{CNT}}$  emitted by the nanotubes (black curve, left vertical scale), as a function of the negative voltage  $V_{\text{CNT}}$  provided to them, compared with the rate of pulses (red markers, right vertical scale) recorded by the TES. The inset shows a typical TES pulse shape for  $V_{\text{CNT}} = 100$  V.

The electrons are emitted from an area much larger than the TES, so the heating created by electrons hitting the nearby environment must be considered. In general, the Joule power  $P_J$  required to bring the TES to its critical temperature  $T_C$  is given by [30]

$$P_{\rm J}(T_{\rm local}) = I_0^2 R_0(T_{\rm local}) = \kappa (T_{\rm C}^n - T_{\rm local}^n), \qquad (2)$$

where  $I_0$  is the current flowing in the TES; the exponential parameter and the coupling constant of this device



FIG. 4. Power  $P_{\rm J}$  needed to bring the TES to its working point (black markers, left vertical scale) and local temperature  $T_{\rm local}$  around the TES device (red markers, right vertical scale) for different values of  $V_{\rm CNT}$ . The bath temperature  $T_{\rm bath} = 41.7$  mK is indicated by the red dashed line.



FIG. 5. Typical spectrum of TES signal amplitudes, obtained with  $V_{\text{CNT}} = 100 \text{ V}.$ 

are respectively measured to be  $n = 4.78 \pm 0.07$  and  $\kappa = (10 \pm 1) \times 10^{-7}$  W K<sup>-n</sup>; and  $T_{\text{local}}$  is the local temperature in proximity of the TES. At low  $V_{\text{CNT}}$  the electron rate is minimal, and therefore  $T_{\text{local}} \approx T_{\text{bath}}$ . As  $V_{\text{CNT}}$  increases, the rate of electrons and the associated energy deposition in the vicinity of the TES increase, raising  $T_{\text{local}}$ . This effect is shown in Fig. 4, where the black markers represent  $P_{\text{J}}$ , as measured from  $I_0$  and  $R_0$ , and the red markers represent  $T_{\text{local}}$ , as obtained by inverting Eq. (2). As can be seen, when operating the electron source at  $V_{\text{CNT}} = 105$  V, the local temperature is already  $T_{\text{local}} > 63$  mK, over 20 mK above  $T_{\text{bath}}$ . This implies that results at different  $V_{\text{CNT}}$  values are not rigorously comparable, as the TES operates under different conditions.

For each value of  $V_{\text{CNT}}$ , the amplitudes of the TES signals are analyzed. A typical spectrum, obtained for  $V_{\text{CNT}} = 100 \text{ V}$ , is shown in Fig. 5: it presents a high-amplitude peak, corresponding to the full absorption of the electrons in the TES; a marked tail to the left of the peak, due to partial absorption of electrons, most likely due to electrons that fail to be stopped by the thin TES bilayer (45 nm); and a low-amplitude peak, truncated by the trigger threshold of 166 mV, compatible with electrons backscattered out of the TES after exciting an internal mode in the Au layer.

We fit the high-amplitude peaks of these distributions with asymmetric Gaussian functions, described by the peak position  $\mu$ , and left ( $\sigma_L$ ) and right ( $\sigma_R$ ) tails. The parameter  $\sigma_R$  is mainly due to the energy resolution of the device. Example fits, for  $V_{CNT} = 97$ , 101, 103, and 105 V, are shown in Fig. 6.

Figure 7 shows the TES Gaussian energy resolution for fully absorbed electrons (red circular markers) and photons (black square markers) as a function of the particle energy.



FIG. 6. Example fits, for four different values of  $V_{\text{CNT}}$ , of the high-amplitude peak with the asymmetric Gaussian function.

The photon energy resolution is defined as the Gaussian widths of the fit shown in Fig. 2. The electron energy resolution is  $\sigma_e = (\sigma_R/\mu) \times E_e$ .

The Gaussian energy resolution, for fully absorbed electrons, is measured to be  $0.8 < \sigma_e < 1.8$  eV for electrons in the  $90 \le E_e \le 101$  eV energy range, and is found to be compatible with that of photons in the same energy range. This is a nontrivial result, as at such low energy these particles have different interactions with matter, and suggests that the heat-based detection mechanism in the TES is the

![](_page_4_Figure_12.jpeg)

FIG. 7. TES electron energy resolution for photons (black square markers) and fully absorbed electrons (red circular markers) as a function of the particle energy.

same for electrons and photons. This casts optimism on the PTOLEMY target of  $\sigma_e = 50$  meV, because this has already been achieved by these devices with photons [4]. Clearly, to develop a high-resolution low-energy electron detector, significant work will be needed to understand the processes that broaden the left side of the absorption peak, and find solutions to limit their impact. Nevertheless, this work marks the beginning of high-resolution electron spectroscopy with TES devices.

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