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Measurement of the Absolute Phase Error of Digitizers

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Abstract—The paper proposes a method for the measurement of digitizer absolute phase errors, defined as the phase displacement between the digitized output and the input analog waveform. The measurement procedure is based on the use of a phase reference signal, which is theoretically synchronous with the input analog waveform and that triggers the digitizing sampling clock. From the characterization of the waveform generator phase response and the measurement of the time delay of the digitizer sampling clock with respect to the phase reference signal, an accurate evaluation of the digitizer absolute phase error is obtained. The method has been applied to a high performance digitizer, measuring the absolute phase errors of two different channels. The expanded uncertainty of the method has been quantified as a few microradians at 50 Hz and 150 μ rad at 20 kHz.

Index Terms—Phase Measurement, Digitizer, Calibration, Power System Measurements, Discrete Fourier Transform, Phasor Measurement Unit, Digital Low Power Instrument Transformer

I. INTRODUCTION

THE knowledge of phase angles of signals is at the base of many engineering applications, from telecommunications to power systems ([1]-[2]). In particular, in most measurement applications, electronic instrumentation is based on digitizers, to convert analog signals to digital samples that are handled by digital signal processors to get the desired measurement value. However, every digitizer has its own phase frequency response which introduces a phase deviation between the analog input and its corresponding digital output samples, that is here defined the absolute phase error of the digitizer. This deviation depends on the characteristics of the digitizer input circuitry and on the digitalization architecture. For very low frequency signals, this phase deviation can be negligible, if the phase displacement reflects into a time delay much lower than time period of the considered waveform. For many applications, two channels of the same digitizer are involved in the measurement at the same time (i.e. power, energy or impedance measurement) so that only the relative phase delay between

channels is important. Measuring the relative phase delay between two channels of the same digitizer, or two channels of two different digitizers with synchronized sampling clocks, is an issue faced in a number of scientific papers ([3]-[5]). However, there are special applications, such as high accuracy calibration of Phasor Measurement Unit (PMU) for medium voltage grid application ([6]-[10]) or calibration of Low Power Instrument Transformers ([11]-[14]) with digital output (carried out by comparison with a standard analog transformer), where high phase accuracies, of the order of the microradian, are required. In these situations, the absolute phase deviation of the single channel of the used digitizer may be comparable or higher than the required accuracy, introducing an unacceptable systematic error that highly influences the measurement result. An interesting technique for the measurement of digitizer absolute phase error was proposed in [15], that involves the generation of a reference signal with known phase with respect to a time reference, but it is not thoroughly discussed and only first results are shown.

In this paper, a different technique for measuring the absolute phase errors of digitizer is presented. The technique has been introduced in [16], but here a thorough theoretical explanation is given, together with an exhaustive uncertainty analysis and an experimental validation. It is based on the preliminary characterization of the phase error of the used analog waveform generator with respect to a phase reference signal (PRS), through the use of a phase comparator ([4]-[5]). By means of a frequency counter, which measures the time delay between the sampling clock of the Digitizer Under Test (DUT) and the PRS, and applying the Discrete Fourier Transform (DFT) to the DUT samples, the absolute phase error of the DUT is measured.

The paper is organized as follows: Section II describes the measurement procedure, whereas Section III focuses on the adopted measurement set-up. Section IV analyses systematic errors and uncertainty contributions. Section V discusses the experimental characterization of a digitizing module and Section VI, in order to validate the proposed technique, presents a comparison with results obtained through a phase comparator ([3]-[5]).

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II. MEASUREMENT METHOD

The measurement of the absolute phase error of a digitizer involves the evaluation of a phase delay between a digitized quantity, that is the output samples of the digitizer, and an analog quantity (typically a voltage), that is the digitizer input signal. At the best of authors' knowledge, direct measurement methods able to quantify this phase error are not available. Therefore, an indirect measurement method, based on the introduction of a reference phase signal (a square wave), having the same frequency of the input signal, has been adopted.

At first, let consider an Arbitrary Waveform Generator (AWG) that also provides a signal that acts as the PRS. This is a square signal with the same periodicity, T_0 , of the generated sinusoidal signal. When a sinusoidal signal s_g is generated, ideally, the zero crossing of the sinewave and square wave should be at the same time instant. Actually, due to the frequency response of the AWG and to its internal time delay, there is a time delay, T_g , between the zero crossing of sinewave and the rise of square wave. Assuming the rising edge of the PRS as the time reference ($t=0$), the time delay, that corresponds to an initial phase angle of the sinewave equal to φ_g , is:

$$\varphi_g(f_0) = \frac{2\pi}{T_0} T_g = 2\pi f_0 \cdot T_g = \omega_0 T_g \quad (1)$$

where f_0 is the signal frequency. Thus, the generated sinewave can be written as:

$$s_g(t) = \sin(2\pi f_0 t + \varphi_g) \quad (2)$$

where, for sake of simplicity, a unitary amplitude is considered. This effect is illustrated in Fig. 1.

Now, let suppose that PRS is used to trigger the starting of the sampling performed by the digitizer to be characterized (Device Under Test - DUT). Ideally the first command should be aligned with the rising edge of PRS, but, due to the delay of the clock paths, it is actually delayed of a time interval, T_c (see Fig.2).

After that, sampling commands are generated equally spaced of

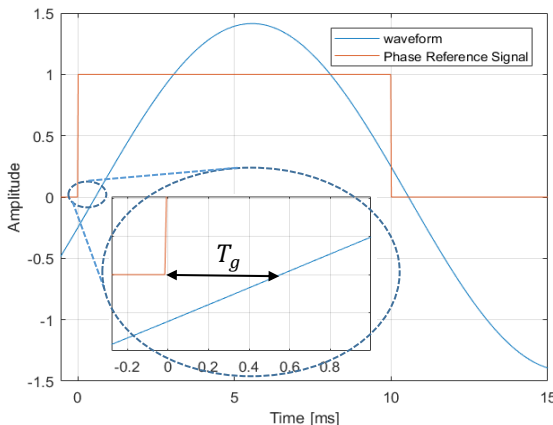


Fig.1. Time delay between sine wave and phase reference signal.

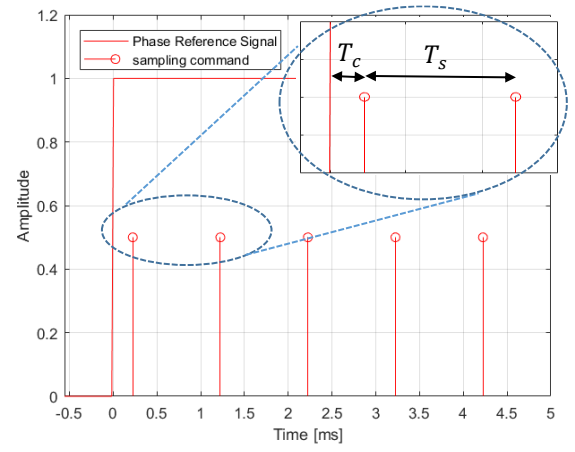


Fig.2. Time delay between phase reference signal and sampling commands.

the chosen sampling period T_s with the accuracy of the adopted sampling clock (Fig. 2).

In a digitizer, the sampling command should ideally produce an instantaneous acquisition of a sample but, actually, there is always a delay T_{DUT}^d between the sampling command and the acquisition of the sampled value. This delay impacts on the acquired waveform as a phase shift. This, summed to the phase shift φ_{DUT}^a introduced by transfer function of the analog input circuitry of the digitizer, determines a phase error, i.e. the absolute phase error of the digitizer (φ_{DUT}). Therefore, the absolute phase error of the DUT can be expressed as:

$$\varphi_{DUT} = 2\pi f_0 T_{DUT}^d + \varphi_{DUT}^a \quad (3)$$

As a consequence, the time delay between the sampling command and the acquisition of the sampled value is

$$T_{DUT} = \frac{\varphi_{DUT}}{2\pi f_0} \quad (4)$$

This situation is depicted in Fig. 3.

In order to evaluate the absolute phase error, let suppose that the DUT is supplied with a signal s_g and the PRS triggers the sampling performed by the DUT. All the phenomena previously shown occur together, as shown in Fig. 4.

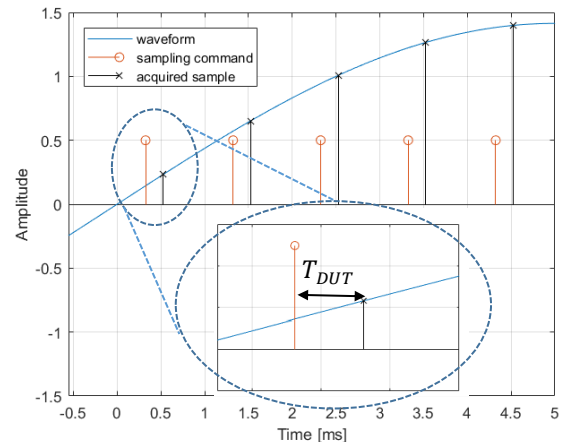


Fig.3. Time delay between sampling commands and acquired samples.

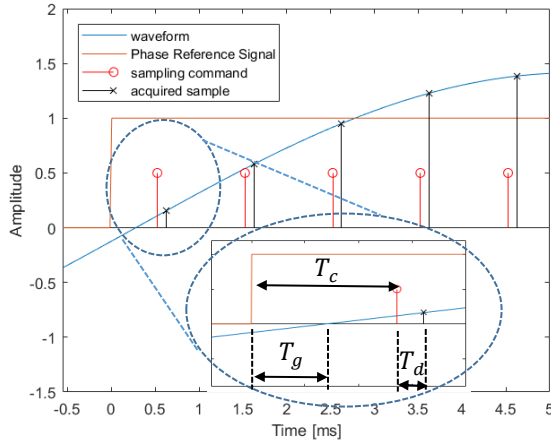


Fig. 4. DUT sinusoidal input, Phase Reference Signal and ideal and actual samples acquired by DUT.

The sinusoidal waveform acquired by the DUT can be expressed as

$$\begin{aligned} s_{DUT}(kT_s) &= \sin\left(2\pi f_0(kT_s + T_c + T_{DUT} - T_g)\right) \\ &= \sin(2\pi f_0 kT_s + \varphi_c + \varphi_{DUT} - \varphi_g) \quad (5) \\ &= \sin(2\pi f_0 kT_s + \varphi_T) \end{aligned}$$

where time delays are given in terms of phase displacements (1). The term φ_T represents the comprehensive effect of all time delays on phase displacement of the acquired sinusoid. The phase angle, φ_T , can be evaluated by performing the DFT on the acquired samples and evaluating the phase angle at frequency f_0 with a synchronized acquisition or different signal processing techniques. The phase deviation φ_{DUT} , introduced by the DUT at frequency f_0 , can be then obtained by

$$\varphi_{DUT} = \varphi_T - \varphi_c + \varphi_g \quad (6)$$

where the phase delays φ_c and φ_g are measured as detailed in the following.

III. MEASUREMENT SETUP

To validate the proposed method a proper automated test bench has been realized. Its block scheme is shown in Fig. 5.

The system is based on a PXI chassis, a GPS-disciplined Rubidium atomic clock (Fluke 910R) and an external universal frequency counter (Agilent 53230A). The multifunction I/O module NI PXIe-6124 (± 10 V, 16 bit, maximum sampling rate 4 MHz) is the DUT. The module NI PXI-5422 (± 12 V, programmable gain, 16 bit, maximum sampling rate 200 MHz) has been used for AWG. The NI PXI 4462 (± 10 V, 24 bit, maximum sampling rate of 204.8 kHz) module is used as a phase comparator.

All the instruments of the test bench operate synchronously, since the clock source from the Fluke 910R is provided to the whole PXI backplane and to the frequency counter as external timebase. Clock signals (with frequency different from 10 MHz) and trigger signals are generated by the

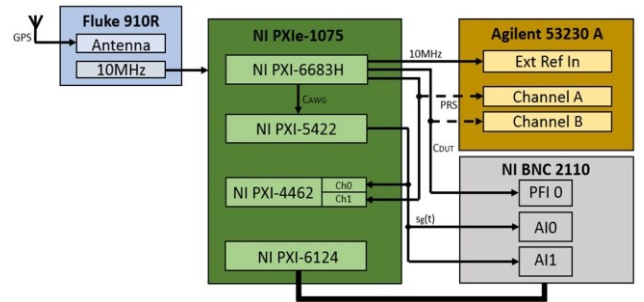


Fig. 5. Measurement setup

NI PXI-6683H synchronization board. In particular, the sampling clock of DUT (C_{DUT} in Fig. 5), the PRS and the AWG generation clock (C_{AWG} in Fig. 5, set to 5 MHz) are generated by the NI PXI-6683H. A digital storage oscilloscope (Lecroy MDA810, not shown in Fig. 5) is used to control the correct operation of the setup and to measure the rise time of the PRS. It is worth to underline that C_{DUT} is externally provided to the DUT, through the terminal PFI0 (Programmable Function Input 0); moreover, the DUT starts to sample when it recognizes the first pulse of the sample clock, which is delayed from PRS of a time T_c (see Fig. 2).

The AWG generating the sinewaves s_g , is connected to both the DUT and phase comparator (COMP), which measures the phase difference φ_g between s_g and PRS. The frequency counter gives the time delay T_c between PRS and DUT sampling clock. All the clock and signal paths are symmetrically managed (as better explained in the following) in order to avoid different propagation delays.

Measurement software is developed in LabVIEW, using the event-based state-machine approach.

For each test point, amplitude and frequency of the test signal of the DUT can be chosen and 30 repeated measurements of φ_T , T_c and φ_g are performed. In order to evaluate φ_T , for each test frequency a time window equal to a fixed number of signal periods is used to perform the DFT.

For the sake of simplicity, in the realized setup a DUT which accepts external sampling clock is used. However, the proposed method does not lose generality even in the presence of a DUT which accepts the sampling clock through the communication bus (whatever it is), since it is sufficient to access to the pin receiving the sampling clock.

IV. SYSTEMATIC ERRORS AND SOURCES OF UNCERTAINTY

A. Counter and Comparator inter-channel delay

Both the measurement values given by the phase comparator, φ_g , and by the frequency counter, T_c , are affected by systematic errors due to differential time delay between the two paths to the channel input of the instruments. These systematic effects can be estimated and corrected as briefly described in the following.

Let consider the two input paths of a frequency counter, as depicted in Fig. 6a: τ'_a and τ'_b indicate the time delays in propagation due the cables that connect the signals to channel A and to channel B, respectively; τ''_a and τ''_b are the time delays due to the conditioning circuits at the inputs stages of channel

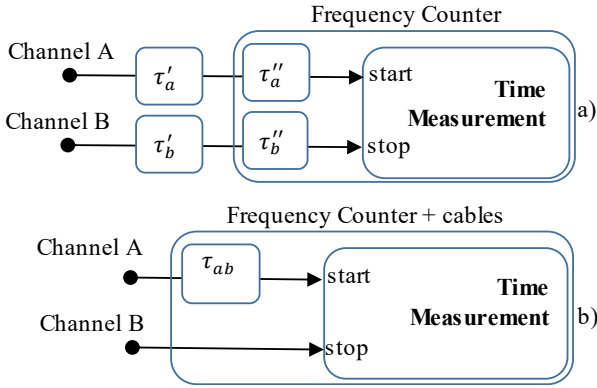


Fig. 6. a) delays at the input channels of a frequency counter; b) cumulative delay representation

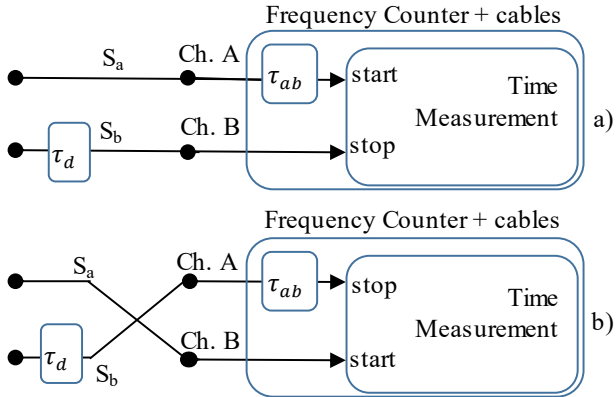


Fig. 7. The differential delay of a frequency counter including cables

A and channel B, respectively. For time measurements that involve both channels, the effects of these delays can be cumulated into a differential delay, τ_{ab} equal to

$$\tau_{ab} = \tau'_a + \tau''_a - (\tau'_b + \tau''_b) \quad (7)$$

and accounted as done in Fig. 6b.

The differential delay τ_{ab} is a systematic delay, at least in a short-term time period, and thus compensated. To this aim, we consider two square signals S_a and S_b with time shift τ_d . Setting S_a as a start and S_b as a stop (Fig. 7a) ΔT_1 is obtained; then, swapping the two inputs and start and stop (see fig. 7b) and repeating the measurement, ΔT_2 is obtained. It is:

$$\begin{cases} \Delta T_1 = \tau_d - \tau_{ab} \\ \Delta T_2 = \tau_d + \tau_{ab} \end{cases} \quad (8)$$

and

$$\tau_d = \frac{\Delta T_1 + \Delta T_2}{2} \quad (9)$$

In this way, performing two measurements and combining opportunely the results, the systematic time delay between channel A and channel B is automatically compensated.

Similar considerations can be done for the phase comparator, considering now that the signals at its inputs have relative phase

delay of $\Delta\varphi_d$. The introduced uncertainty contribution depends on the repeatability and stability of the generated signals. In this case, the systematic effect introduced by the comparator, can be modelled with a differential phase displacement, $\Delta\varphi_{ab}$.

Performing two measurements, inverting the inputs, the (10) is obtained. It results:

$$\begin{cases} \Delta\varphi_1 = \Delta\varphi_{ab} + \Delta\varphi_d \\ \Delta\varphi_2 = \Delta\varphi_{ab} - \Delta\varphi_d \end{cases} \quad (10)$$

B. Time delay between DUT sampling clock and PRS

As it is explained in Sec. II, the rising edge of the PRS is considered as the time reference ($t=0$) and, thus, all the measured time or phase delays are referred to it. However, an uncertainty source has to be considered as associated to this assumption, that is the fact that the PRS is not an ideal square wave; this aspect particularly affects the measurement of the time delay between the DUT sampling clock and the PRS. In fact, the intrinsic low-pass behavior of the PRS generation affects amplitudes and phases of all harmonic components of the generated square wave, possibly introducing phase delays. Nevertheless, if the analog bandwidth of the PRS generator is sufficiently greater than the fundamental frequency of the generated square wave, then the contribution to the total uncertainty, due to this assumption, can be considered small. For the case at hand, the square waves (PRS and DUT sampling clock) are generated by the synchronization board, which is optimized to deal with square waves and has an analog bandwidth of about 50 MHz, whereas the maximum analyzed frequency is 20 kHz, that is more three orders of magnitudes lower. However, measuring the rise time of the PRS, the estimated uncertainty contribution is lower than $0.2 \mu\text{rad}$ at 50 Hz and $68 \mu\text{rad}$ at 20 kHz.

C. Phase delay between sine wave and PRS

From a mathematical point of view, the phase is defined for a sine wave with respect to a time reference. Therefore, the problem of measuring the phase delay between the sine wave and the PRS is ill-posed. It is more correct to consider the time delay between the rising edge of the PRS and the zero crossing, with positive slope, of the sine wave. Then it is straightforward to think to employ a frequency counter to measure this time delay. However, the frequency counter, in order to measure the time delay between two signals, adopts trigger circuits to “square” the two waveforms. Especially with low frequency signals, as in the case here considered, characterised by a low slope in correspondence of the zero crossing, the trigger circuits can introduce an unacceptable uncertainty.

However, it can be analytically demonstrated that the positive zero crossing of the fundamental component of a square wave is coincident with the rising edge of the square wave. Therefore, the problem can be simplified by measuring the phase delay between the sine wave and the fundamental component of the square wave, through the use of a digital phase comparator.

The fundamental component of a square wave can be

obtained with a suitable analog filter. However, it is well known that analog filters introduce noise, could have problems of time stability, which influences the repeatability of the measurements. Moreover, their characteristics could be very sensitive to the environmental conditions.

The phase delay between the sine wave and the PRS is here measured in the frequency domain, performing the Discrete Fourier Transform on the samples of the two waveforms; this is possible since the considered signals are stationary. As it is known, the frequency spectral content of a square wave is infinite and, thus, the effect of the finite sample rate causes aliasing. This, in turns, makes some of the aliased high frequency components (the harmonic frequencies that differ from a multiple of the sampling frequency by an amount exactly equal to the fundamental frequency) sum up to fundamental tone, causing the modification of the fundamental phase angle and, therefore, making the measurement less accurate.

This problem was here solved using a digital antialiasing filter, with variable order (depending on the chosen sampling rate) and cut-off frequency equal to about half of the chosen sampling rate; the filter is internal to the COMP and is applied to all COMP inputs. In this way, assuming that the chosen COMP sampling rate is sufficiently higher than the PRS fundamental frequency (as in this case), 1) the aliasing problem is prevented, 2) the Nyquist theorem is respected for the fundamental component of the PRS and, thus, 3) the phase angle of the fundamental tone of the PRS is correctly evaluated.

Nevertheless, an uncertainty source, due to the fact the two input channels of the COMP are stimulated with waveforms with different characteristics, i.e. a sine wave and a square wave, has to be considered. In particular, the square wave could stimulate a residual non-linear behavior of the channel, which is not stimulated by the sine wave.

In other words, the hypothesis at the basis of the compensation of the inter-channel phase delay, explained in Section V.A, is the linearity of the input channels of the COMP. If signals that stimulate non-linear behavior of the channels are used, then the inter-channel phase delay cannot be compensated in the way it is explained. Nevertheless, two comments are due.

First of all, the used digitizer for the COMP ([18]) has very good linearity and noise performances and so its main behavior can be considered very linear. Moreover, even if a residual non-linear behavior can be faced when using square waves, it is not a simplification to assume that the non-linear behaviors of the two channels is the same.

If these two hypotheses are true, considering again the signals in Section V.A and assuming that the signal b is the fundamental component of the PRS, then equations (10) can be rewritten as follows:

$$\begin{cases} \Delta\varphi_1 = \Delta\varphi_{ab} + \Delta\varphi_d + \Delta\varphi_{1,NL} \\ \Delta\varphi_2 = \Delta\varphi_{ab} - \Delta\varphi_d + \Delta\varphi_{2,NL} \end{cases} \quad (11)$$

where the values $\Delta\varphi_{1,NL}$ and $\Delta\varphi_{2,NL}$ are the additional phase displacement due to the square wave when it is applied to the first and to the second channel, respectively. Since we have assumed that $\Delta\varphi_{2,NL} = \Delta\varphi_{1,NL}$, then the equation (10) is still

valid.

The contributions of these assumptions to the total uncertainty is quantified to be lower than 0.1 μrad at 50 Hz and 32 μrad at 20 kHz. It has been estimated by measuring the mismatching between the relative phase error of the two channels: 1) when they measure the same sine wave and 2) when they measure the same square wave.

D. Uncertainty on sampling event of the DUT

Another source of uncertainty is represented by the time instant in which the DUT, that receives a sampling clock pulse, performs the sampling. It is worthwhile noting that, to the aim of the analyses made in this subsection, the jitter and the noise of the sampling clock are not considered.

From the datasheet of the DUT ([19]), it is known that it recognizes a sampling command when the rising edge of the sampling clock reaches the value of about 2.2 V.

Therefore, a combined contribution to the total uncertainty is considered given by 1) the not perfect vertical rising edge of the sampling clock and 2) the not perfect recognition of 2.2 V by the DUT. With the frequency counter the time interval between the sampling clock crossings for 2.1 V and 2.3 V has been measured. Its uncertainty contribution has been quantified to be lower than 10 nrad at 50 Hz and 4 μrad at 20 kHz.

E. Distortions on high frequency content signals

When a square signal, sampling clock or PRS, is connected to two measuring systems with high input impedance, as required by the procedure (Fig. 5), a strong distortion arises at the edge of such signals.

This distortion introduces a high variability in the time delay measurements. However, no significant distortion has been detected when the square signal generator is connected to only one measuring system.

So, under the assumption of good short-term stability of the generation and acquisition system, the measurements have been performed in sequence.

F. Uncertainty budgets

Starting from the analysis of the systematic errors and the uncertainty sources, shown in the previous subsections, the uncertainty budget is quantified in Table I. It summarizes all the standard uncertainty contributions, where all the repeatability and stability contributions are summed up.

V. EXPERIMENTAL RESULTS

The DUT is tested in a variety of conditions. Four different signal amplitudes (1 V, 2 V, 5 V, 10 V), corresponding to four

TABLE I. STANDARD UNCERTAINTY CONTRIBUTIONS

Source		Frequency [Hz]	
		50	20k
φ_T	[μrad]	0.01	4
φ_c		0.2	68
φ_g		0.1	32
Repeatability and stability		1.5	1

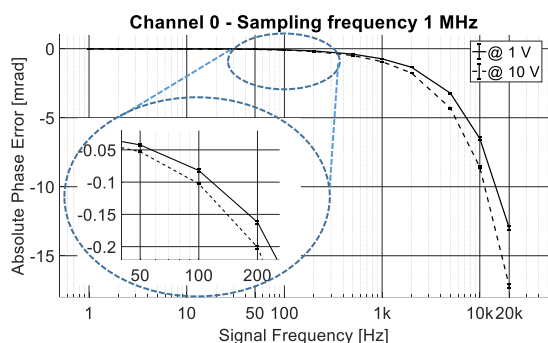


Fig. 8. Absolute phase error of the channel 0 of the DUT, when sampling frequency is fixed to 1 MHz and signal amplitude and frequency change.

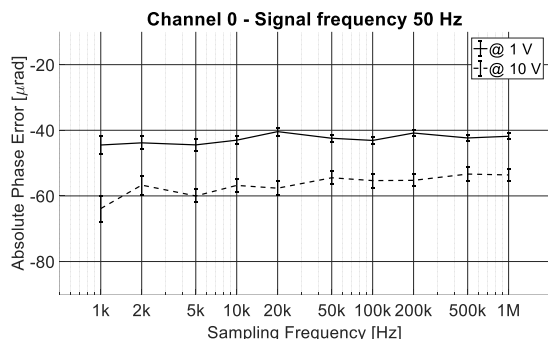


Fig. 9. Absolute phase error of the channel 0 of the DUT, when signal frequency is fixed to 50 Hz and signal amplitude and sampling frequency change.

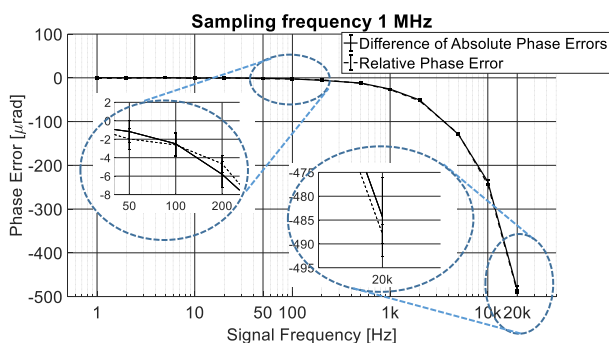


Fig. 10. Comparison between the difference of the absolute phase errors of channel 0 and channel 1 and their relative phase error. Sampling frequency is fixed to 1 MHz and signal amplitude and frequency change.

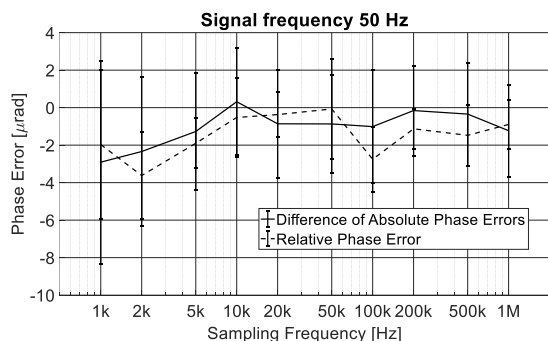


Fig. 11. Comparison between the difference of the absolute phase errors of channel 0 and channel 1 and their relative phase error. Signal frequency is fixed to 50 Hz and signal amplitude and sampling frequency change.

different DUT input ranges, have been used.

Signal frequencies from 1 Hz to 20 kHz have been considered. Two sets of tests have been performed. In the first set, the DUT sampling frequency has been set to 1 MHz and the signal frequency has been varied.

In the second set, the signal frequency has been fixed to 50 Hz whereas DUT sampling frequency has been changed from 1 kHz to 1 MHz.

Tests have been performed for two DUT channels (CH0 and CH1). Here, for sake of brevity, only the results related to CH0 are shown.

Fig. 8 show the results of the first set of tests, referring to 1 V and 10 V ranges only; the results for 2 V range and 5 V ranges are very similar to those of 10 V range. The inset shows a zoom between 50 Hz and 200 Hz. The performances of the channel slight decrease passing from range 1 V to range 10 V. Fig. 8 shows also the expanded uncertainty (level of confidence 95%). In the considered situation, CH0 exhibit an absolute phase error lower than 10 mrad till 10 kHz. The expanded uncertainty is about 4 μ rad at 50 Hz and 150 μ rad at 20 kHz.

In Fig. 9 the results of the second set are shown. Also in this case smaller errors have been found at 1 V, about -43 μ rad, with respect to 10 V, about -60 μ rad. The behaviors of the other ranges are very similar to each other, with performances slightly lower than those found for the first range. The increase of sampling frequency over a few kilohertz does not produce remarkable improvement in terms of uncertainty. In fact, the expanded uncertainty (level of confidence 95%) is 4 μ rad for every sampling frequency.

VI. VALIDATION WITH PHASE COMPARATOR MEASUREMENTS

In order to demonstrate the validity of the proposed method, an experimental comparison with results obtained by a digital phase comparator was performed.

The relative phase delay between DUT channel 0 and channel 1 has been measured in two different ways: a) as a difference between the absolute phase errors (each measured through the procedure described in the previous section) and b) measuring directly their relative phase delay by a previously characterised phase comparator. The same method described in Section IV.B is used to measure the relative phase delay between channel 0 and channel 1 of the DUT. The same signal has been input to channel 0 and channel 1, samples are simultaneously acquired, DFT is applied to the samples and the phase difference of the fundamental components is evaluated. The same two sets of tests discussed in the previous section have been performed. Fig. 10 shows the results of the first set of tests, whereas Fig. 11 deals with the results of the second set. Fig. 10 shows also two insets, where the zooms around 50 Hz and around 20 kHz are shown.

The values estimated with the two methods are always in a very good agreement. Maximum deviations are within 2 μ rad at 50 Hz and 6 μ rad at 20 kHz. The measurement results are always compatible within their uncertainty, considering the correlation due to use of same frequency counter and the PRS. The expanded uncertainty (level of confidence 95%) of the difference of the absolute phase errors, is lower than 5 μ rad

whereas that of the relative phase error, given by the comparator is lower than $1.6 \mu\text{rad}$ up to 20 kHz.

VII. CONCLUSION

In this paper a method for the measurement of the absolute phase error of a digitizer, defined as the phase displacement between the digitized output and the input analog waveform, is presented. The method is based on the use of a phase reference signal (a square wave), synchronous with the input sine wave, and on the characterization of the phase frequency response of the employed arbitrary waveform generator. The method has been applied to a high performance digitizer (10 V, 16 bit, 4MHz), measuring the absolute phase errors of two different channels. The expanded uncertainty of the method has been quantified as $4 \mu\text{rad}$ at 50 Hz and $150 \mu\text{rad}$ at 20 kHz. Good agreement within a few microradians up to 20 kHz has been also found when results of phase differences have been compared with those obtained by a phase comparator.

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