Pantograph-to-OHL Arc: Conducted Effects in DC Railway Supply System

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(Article begins on next page)
Abstract— The electrical arc occurring in the sliding contact between the supply contact line and the current collector (pantograph) of an electrical locomotive is a fast transient phenomenon able to degrade progressively the line-to-pantograph contact quality and consequently the continuity of operation. In order to increase the energy efficiency of the railway system, an inexpensive solution is constituted by the detection of the arc event by the analysis of voltage and current measurements already available on-board train. An essential activity to reach this objective is to set up a reliable electrical model of the railway system in which the arc events originate. To this end, this paper presents a combination of experimental and simulation analysis for the development of an electrical model of a DC 3 kV railway system, which is aimed at better understanding the propagation of conductive effects generated by arc events. First, a laboratory experimental activity is carried out to investigate the electrical dynamic characteristics of the arc in a controlled environment. Then, a model of the DC railway system is derived and validated by using experimental data collected in a measurement campaign on-board train. Finally, a sensitivity analysis on main model parameters is carried out.

Keywords — Voltage measurement, current measurement, DC railway system, Electric arc, rail transportation, pantograph–catenary, predictive maintenance

I. INTRODUCTION

In the majority of the electric railway systems, the power is transferred from the supply to the traction unit (locomotive or electro-train) through a sliding contact between the OverHead contact Line (OHL) and the pantograph. The latter is a servo-actuated current collector placed on the train roof, that applies and controls the force of the contact strip against the contact line. The large power (up to about 8 MW) to be transferred from the OHL to the carbon blade of the pantograph through a contact section of a few square millimetres makes the current collection as one of the most critical elements of the electrical railway power chain [1]. The increasing speed of commercial trains associated with the higher and higher power of the traction units requires advanced predictive maintenance techniques to prevent degradation of the sliding contact and consequent failure of the overhead contact systems [2]. A lively research activity related to the arc modelling in power systems aims at preventing failures and dysfunctions [3]. More specifically, the attention is directed to the accurate estimation of the induced effects produced by arcing in the railway systems [4][5], to the analysis of the contact strip degradation with different material composition [6] and to the influence of some parameters affecting the arc phenomena, i.e. the power factor [7], the direct current (DC) polarity [8], etc... The majority of such works addressed alternating current (AC) railway supply systems, neglecting DC systems. The research activity presented in this paper, conversely, is focused on DC systems. It has been developed in the framework of the EMPIR 16ENG04 MyRailS research project, which aims at developing the metrological framework to foster the energy efficiency in railway systems. In particular, one of the objectives of this project is to develop a measurement technique to detect the presence of arc phenomena starting from the analysis of voltage and current measurements already available on-board train: the goal is to allow the predictive maintenance based on a continuous monitoring of the arc events, which degrade the overhead contacts and thus decrease the energy efficiency of the whole railway systems, without the need of additional specific measuring devices and so without additional costs. An essential activity to reach this objective is to set up a reliable electrical model of the system in which the arc events originate, which is constituted by the DC railway Electrical SubStations (ESSs), the OHL, the locomotive and the measuring system. Therefore, this paper is focused on the development of a reliable electrical model aimed at understanding the behavior of voltage and current signals during arc events; the approach adopted, summarized in the following, is a combination of experimental and modelling activity. Section II studies the dynamic electrical characteristics of the arc, by performing laboratory experimental tests in a controlled environment. In Section III, the characteristics of the arc behaviour are identified, as well as the structure of the circuitual model of the railway system, thanks to the information provided by RFI (Rete Ferroviaria Italiana, the Italian railway infrastructure owner). Then, in Section IV the model is validated by using experimental data collected in a measurement campaign on-board train, performed on a high-speed electro-
train, model ETR 600, and made available by Trenitalia (the largest Italian railway operator). Section V deals with a sensitivity analysis on the main model parameters. Finally, Section VI draws the conclusions.

II. THE DYNAMIC V-I ARC CHARACTERIZATION

As highlighted in the introduction, in scientific literature a few papers deal with the voltage behavior of an electric arc occurring between the OHL and the pantograph in a DC 3 kV railway system. Therefore, an experimental setup, reproducing a sliding contact similar to that occurring in a railway system, has been realized: the aim is to analyze the dynamic behavior of voltage and current, related to the sliding contact, in order to define the voltage profile of the arc, that is the input of the electrical model developed in Section III.

A. Effects of pantograph arcing on railway systems

Pantograph arcing is a common phenomenon in electrified railway systems. It is a source of broadband-conducted and radiated electromagnetic interference (EMI) for the vehicle, as well as for traction power and signaling systems [9]. Additionally, the arcing phenomenon produces a localized very high temperature (10000 K to 13000 K), so that corrosion spots of both pantograph and OHL [10] may occur. Therefore, intensive and prolonged arcing phenomena can damage not only the pantograph strip, but also the OHL which can, in turn, accelerate the wear of pantograph of other trains running on the same line section. Moreover, arcing phenomena can produce damped oscillations on the over-head feeder with frequency content of some kilohertz [11].

B. Brief description of the arc phenomena

An arc is defined as an electric discharge occurring in a conductive ionized gas between two electrodes [12]. The conductive nature of the gas is provided by the plasma between the electrodes, namely a combination of positive ions and free electrons moving in a high temperature region. As depicted in Fig. 1, the ionized gas between the two electrodes can be divided in three regions: anode region, plasma column and cathode region; each region is characterized by a different voltage profile. A constant gradient describes the voltage profile in the plasma column, while a non-linear voltage profile is observed for both the anode and cathode regions, where the transition occurs between the solid state of the electrodes and gaseous plasma cloud [12]. For static electrodes, the sum of voltage drops across the two transition regions only depends on the electrode nature.

A typical voltage-current (V-I) characteristic of a DC arc with a specific length is shown in Fig. 2. At very low current (tens of amperes) a behavior defined by a constant arc power law can be observed; for currents higher than a specific threshold the voltage level does not depend any longer on the current value. Various V-I characteristic curves for DC low-voltage arcs with static electrodes are provided by Paukert’s [13]: he collected data provided by seven research institutes for current ranging from 100 A to 100 kA as shown in Table I.

![Fig. 1. Voltage drop behavior on the arc length](image1)

![Fig. 2. V-I characteristic of a stationary electrical arc](image2)

<table>
<thead>
<tr>
<th>Electrode gap [mm]</th>
<th>$V_{arc}$ [V]</th>
<th>$V_{arc}(I_{arc}=100A)$ [V]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>13.04·$I_{arc}^{0.086}$</td>
<td>20.5</td>
</tr>
<tr>
<td>5</td>
<td>14.13·$I_{arc}^{0.211}$</td>
<td>37.3</td>
</tr>
<tr>
<td>10</td>
<td>16.68·$I_{arc}^{0.168}$</td>
<td>35.3</td>
</tr>
<tr>
<td>20</td>
<td>20.11·$I_{arc}^{0.100}$</td>
<td>48.2</td>
</tr>
</tbody>
</table>

Experimental results presented here have been measured under different dynamic conditions with respect to Paukert’s experiments, so that a direct comparison is not immediate. Anyway, compatible results have been obtained, as it will be demonstrated in the following.

C. Setup of the arc generator

The experimental setup employed in this work was arranged at INRIM in the 90s for a research project devoted to the analysis of the electromagnetic field at high frequency emitted by the arcs generated between two sliding contacts [4] (see Fig. 3 and Fig. 4).

The elements of the sliding contact, namely OHL and pantograph, are emulated by the profile of a 60 cm diameter copper disk, coupled with the shaft of a DC motor (maximum speed 2π·50 rad/s, that is 3000 rpm) and a real pantograph sliding element. The pantograph is kept against the copper disk edge by means of a weight that, thanks to a leverage system, provides the correct contact pressure. Moreover, a crank connecting-rod system moved by a compressed air actuator, which allows an alternative horizontal translation of the pantograph, simulates the zig-zag arrangement due to staggering of the real OHL. Different speeds of the locomotive
sliding contact are obtained by varying the motor rotational speed.

The sliding contact is supplied at an almost constant DC voltage. The electrical current flows from the positive pole of the supply system to the rotating disk through a brush system and then, through the sliding contact, to the pantograph, which is connected to the negative pole of the supply. A series connected 156 μH inductor (resistance of 3.59 mΩ) is used to sustain the arc at the sliding contact.

With the leverage system it is possible to reduce the contact pressure of the pantograph against the copper disk until it is completely detached and arc injection begins. Then, distance may be further increased at the point that the arc quenches. An example of arc evolution is shown in Fig. 5.

Different supply conditions and rotation speeds correspond to different quenching distances and arc characteristics. The experimental setup is used to generate arcs with controlled and repeatable parameters and under conditions as close as possible to those that can be found in a DC railway supply system.

D. Experimental results

Three electrical quantities have been recorded: the current flowing in the circuit, \( I_{\text{arc}} \), the voltage drop across the sliding contact, \( V_{\text{arc}} \), and the DC voltage at the power supply, \( V_{\text{dc}} \). These quantities have been recorded by means of an acquisition system with sampling frequency 10 kHz. The acquisition system is based on a DEWETRON platform with DAQP-DMM signal conditioners, insulation level up to 1.5 kVrms and bandwidth larger than 25 kHz; the current transducers are the Chauvin Arnoux PAC12 clamps, suitable for DC and AC current measurements, with 5 kHz bandwidth. The electrical characteristics of the arc events are shown in Fig. 6 and Fig. 7 and they were obtained with a speed rotation of the disk \( n = 1230 \) rpm corresponding to a simulated speed \( v \) of the locomotive of 139 km/h. When a good contact is present between the disk and the pantograph, the time behavior of the current in the circuit follows the typical inductor transient charging (see (1) and Fig. 6) with an exponential increasing of current under constant voltage supply of an R-L circuit. When the arc occurs, a sudden voltage drop, \( V_{\text{arc}} \), appears in the circuit and the current time behavior follows the typical inductor transient discharge; in other words, the energy stored in the inductor is spent to keep up the arc between the disk and pantograph (see (2) and Fig. 6). For sake of brevity, the analytical formulation describing this phenomenon is provided for the first two time intervals, \( 0 – t_1 \) and \( t_1 – t_2 \) highlighted in Fig. 6. The application of the Kirchhoff’s voltage law to the single loop circuit shown in Fig. 3 provides the current behavior for the two time intervals:

\[
i(t) = \frac{E}{R} \left( 1 - e^{-t/\tau} \right) \quad \text{for} \quad 0 < t < t_1
\]

\[
i(t) = \frac{E - V_{\text{arc}}}{R} \left( 1 - e^{-\left( t - t_1 \right)/\tau} \right) + \frac{I_0}{R} \cdot e^{-\left( t - t_1 \right)/\tau}
\]

(2)

where \( \tau \) is the system-time constant and is defined as \( \tau = L/R \), being \( R \) the equivalent series resistance that takes into account the stray resistance of the inductor \( L \) and the cable connection resistance, \( I_0 \) is the current at time \( t = t_1 \). For the arc events in Fig. 6, a \( V_{\text{arc}} \) of about 16 V – 17 V was measured, that is a value higher than the supply voltage. This is due to the contribution provided by the inductor during its discharge, as demonstrated by the good overlap between computed and measured arc current (see Fig. 6).

From the formula provided in Table I we can give a rough estimation of the arc length. As an example, the first arc occurrence shown in Fig. 6 (\( V_{\text{arc}} = 16.5 \) V) has a length of about 1 mm or less. The onset of arc events at the sliding contact and their characteristics (duration, length) are random. This fact produces a random current chopping with frequent interruption of the electrical circuit (Fig. 7 provides an example).

It can be seen that with good electric contact and nearly zero voltage drop the current increases, but its profile is “chopped” or reverses when arc events are triggered, accompanied by an arc voltage between 15 V and 25 V; longer arcs (in terms of length) require higher arc voltage and consequently a faster decrease of the current. The arc is broken when the energy...
stored in the inductor used to sustain the arc is finished (see Fig. 7 at t=10.5 ms).

Several arc events have been collected during each experimental tests. Fig. 8 shows some V-I behaviors associated with the arc events with random characteristics (length and duration) recorded during the test carried out with a simulated locomotive speed of 139 km/h. Since the high number of arc event detected during the test, the current is strongly chopped. This means that the majority of events occurs at relatively low current (~ 70 A – 80 A). The high curve density shown in the left bottom corner of Fig. 8 highlights this phenomenon. A direct comparison between such behavior and the qualitative behavior provided in Fig. 2 is not possible since the electrodes of the setup are moving. Nevertheless, it is evident that for each recorded arc event, two different V-I behaviors can be distinguished, one at higher currents, where the voltage has a lower slope, and one for lower currents, where the voltage slope is steeper. In many cases, at very low current, the voltage tends to fall down: this is the effect of arc quenching due to a limited energy available in the test circuit.

The experimental set-up is expected to have good scaling capabilities with respect to an actual scenario that has higher power and larger inductance. Its main limit is due to the mechanical rigidity of the disk. In fact, overhead contact lines have a certain amount of elasticity resulting in movement and oscillations under the pressure exerted by the pantograph. This dynamic mechanical behavior is not reproducible with the described system. Anyway, the effect of these oscillations will be taken into account in the following. In real railway systems, a larger supply voltage and inductance can sustain long arc with higher transferred power. On the contrary, such a setup, with an inductance of two orders of magnitude lower than the real one and a lower voltage supply, is not able to sustain long (in terms of time and length) arc events.

However, some general considerations, useful for the comprehension of the real arc event considered in the following, can be deduced. For short arc event, about one millisecond, the arc voltage is constant during the event with an amplitude of about 15 V – 20 V and does not depend on the current flowing in the arc. Moreover, the arc elongation generates a fast increase of the arc voltage (Fig. 7). Such time behavior strongly depends on the mechanical dynamics of the sliding contact, the stochastic path of the arc and the environmental conditions.

III. MODEL DESCRIPTION

A complete circuital model, involving the DC railway supply system, the overhead feeder of the Pisa – Collesalvetti line (Italy) and the input stage of the high-speed electro-train ETR 600 has been developed thanks to information provided by RFI and Trenitalia, respectively. The supply voltage, the absorbed/injected current at the pantograph and the speed of the high-speed train, measured during an approval test performed on the modeled railway line in 2008, have been provided by Trenitalia. Information on the adopted measurement setup was also made available.

A. Test site

The line Pisa - Collesalvetti is a 30 km single track electrified railway line at 3 kV DC with a low gradient; the maximum allowed speed is 150 km/h. It was chosen as a test line because of its weak supply system compared with the large power of the train under test. The equivalent cross section of the line feeder is 400 mm² which in relation with the large train power causes a significant voltage drop. These conditions aim
at stressing the behavior under weak supply voltage conditions as per EN 50388 standard [14].

The railway line is supplied by two ESSs separated by 20 km. The OHL is made of two overhead contact wires, each of 100 mm², sustained by a catenary made of two additional 100 mm² wires. The track has standard 1.435 m gauge with UNI60 rails. The two ESSs have an installed power of 2x3.6 MW each. The output of the AC/DC converter placed in the substation is connected to an L-C 2nd order low pass filter (see Fig. 9) that attenuates the ripple provided by the AC/DC converters. The filter stage is composed of a series connected inductor of 6 mH and a capacitor bank providing 350 µF connected to the return of the DC supply (see Fig. 9).

**TABLE II. VOLTAGE DIVIDER PARAMETERS**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>R&lt;sub&gt;IN&lt;/sub&gt;</td>
<td>6 MΩ</td>
</tr>
<tr>
<td>R&lt;sub&gt;L&lt;/sub&gt;</td>
<td>5.9 kΩ</td>
</tr>
<tr>
<td>C&lt;sub&gt;IN&lt;/sub&gt;</td>
<td>790 pF</td>
</tr>
<tr>
<td>C&lt;sub&gt;L&lt;/sub&gt;</td>
<td>787 nF</td>
</tr>
<tr>
<td>R&lt;sub&gt;OUT&lt;/sub&gt;</td>
<td>50 Ω</td>
</tr>
</tbody>
</table>

**B. The train under test**

The electro-train under test is the high speed ETR600 class built by Alstom. It can be supplied by the AC 25 kV - 50 Hz system, the DC 3 kV or 1.5 kV systems, or the AC 16.7 Hz - 15 kV system. The installed power is 5.5 MW and the train can reach a maximum speed of 250 km/h. The traction architecture is composed of two identical sections, constituted by two three-phase electrical motors. When the train operates under the 25 kV - 50 Hz system, a 25 kV / 3 kV transformer (one for each traction section) reduces the supply voltage; the secondary is composed of two windings supplying two AC/DC converters that are parallel connected on the DC side. The DC bar supplies two DC/AC three-phase converters that feed two electrical motors.

Under a DC supply, the traction system is re-configured in order to introduce at the input stage two series connected L-C low pass filters (see Fig. 10).

The first filter has a resonance of 10 Hz provided by an inductance of 45 mH and a capacitance of 5 mF; the second section has a resonance frequency of 100 Hz with inductance of 0.507 mH and capacitance of 4 mF [15]. The role of this filter is to attenuate the impulsive current absorbed by the DC/AC converters and to reduce harmonic emissions, which are disturbances also for signaling and telecommunication circuits. For trains with double AC and DC supply modes, the on-board transformer is used also to implement the input filter required for DC systems. When the train is running under the DC supply system, the primary of the transformer is open while the current absorbed by the pantograph flows in the first winding of the secondary and, through a counter-series connection (differential connection), to the second winding of the secondary. Thanks to this configuration, the iron core of the transformer experiences a null magnetic flux and the windings provide their contribution to the total inductance of the first stage of the input filter by means of their leakage flux. Two air-inductors series connected provide the remaining inductance necessary to achieve the value of 45 mH.

**C. Measurement setup**

The measurement architecture employed by Trenitalia for these tests was constituted by a resistive-capacitive voltage divider for the measurement of the voltage at the pantograph and a shunt for the total current absorbed by the train. The signals at the output of the two transducers are sent to a National Instrument PXI module through a digital optical link and a data acquisition module (DAQ), as shown in Fig. 11. The values of the divider circuital components are provided in Table II. The bandwidth of the divider is about 20 kHz. For what concern the optical link it has an analog bandwidth of 20 kHz.

**D. Overview on the measurement data**

The quantities measured at the pantograph are shown in Fig. 12. The voltage drop occurring when the train absorbs a large current highlights the feeder resistance and its limited short circuit power.

The voltage provided by the ESSs can be estimated when the absorbed current is almost zero. In fact, since such
measurement campaigns are performed when there is no traffic along the line, an absorption of zero current from the train under test (occurring when train is at standstill or in the coasting phase) allows to estimate the ESS voltage $V_0$ that is close to 3.7 kV. The maximum voltage drop experienced is about 1200 V and occurs for an absorbed current of about 1500 A. These considerations allow the estimation of the equivalent resistance of the feeder supplying the train.

An interesting event has been recorded at time $t = 906$ s: the voltage transient event and its frequency spectrum are provided in Fig. 13, showing that the transient has a typical dumped oscillation with a frequency of about 3.3 kHz. After about 4 ms a new oscillation of lower amplitude is triggered, but disappears immediately.

E. System electrical model

The circuitual model, developed in PSPICE, is shown in Fig. 14. The two OHL sections are simulated as lossy distributed-parameter lines [15]. The electrical parameters of the voltage divider and of the traction line are shown in Table II and III [16].

Since the focus is on the transient events, the only applied voltage is that of the arc event, with the 3 kV DC bias fed by the two substations neglected and replaced by a short circuit. The DC supply voltage amplitude will be added to the computed output voltage in order to perform the comparison with the real measurements.

F. Measurement filter

The Italian procedure for the evaluation of harmonic distortion of the current and voltage waveforms requires a bandwidth of about 4.3 kHz [17]. The real acquisition system is simulated by introducing a 2nd order filter. After several computations and comparisons with the actual voltage waveform, the resonance frequency of the filter has been fixed equal to the observed oscillation frequency of the damped voltage transient, i.e. 3.3 kHz. In order to improve the fit

\begin{table}[h]
\centering
\caption{Electrical parameters of the traction line}
\begin{tabular}{ccc}
\hline
$L_{OHL}$ & 0.57 $\mu$H/m \\
$R_{OHL-DC}$ & 0.17 m$\Omega$/m \\
$C_{OHL}$ & 20 pF/m \\
$G_{OHL}$ & 100 MS \\
\hline
\end{tabular}
\end{table}
between computation and measurement, the overshoot produced by the filter has been emphasized. The inductance of the filter is fixed to $L_{\text{filt}} = 20 \, \text{mH}$. As it is shown later, this quantity strongly affects the behavior of the computed voltage at the output of the measurement chain.

G. Model of the arc event

Following the conclusions of Section II, the arc event, which is the input to the model, has been introduced as an impulsive voltage source connected between the OHL and the input stage of the train. Different shapes of this voltage source have been considered in order to identify the transient arc event that best fits the measured data.

As detected experimentally in Section II, the arc ignition voltage is about $15 \pm 20 \, \text{V}$. With the increase of the arc length, whose amplitude and duration depend on the dynamics of the sliding contact, the arc voltage increases too (see Fig. 7). In the experimental case, the increase of the arc voltage, as a consequence of the arc elongation, is only possible thanks to the energy stored in the series inductance. When the inductance is completely discharged, we observe the arc quenching. In a real railway system, the system supply circuit at $3 \, \text{kV}$ generally is able to feed the arc allowing the dynamic evolution of the sliding contact without arc quenching. According to these considerations, the estimated arc voltage that provides the best fit between measurement and simulation (i.e. the optimized arc voltage profile) has the time behaviour approximately reproducing the arc voltage profile detected in the experiment described in Section II (see Fig. 15).

After a first fast detachment of the pantograph from the OHL, described by the fast increase of the arc voltage, a slower mechanical oscillation of the pantograph occurs. This oscillation is roughly reproduced by the linear increase and successive decrease of the arc voltage shown in Fig. 16, where we see the complete time behaviour of the arc voltage. The overall duration of the event is $4 \, \text{ms}$. After a fast arc voltage increase, $230 \, \text{V}$ in $100 \, \mu\text{s}$, and a fast decrease, $180 \, \text{V}$ in $100 \, \mu\text{s}$, a slower oscillation occurs.

IV. Model Validation

Two different arc voltage profile have been applied, as input, to the proposed model: a rectangular pulse and the optimized arc profile, as shown in Fig. 17.

Fig. 19 compares the simulated behavior obtained with the optimized arc voltage profile and the rectangular one with the measured oscillation.

The rectangular pulse is a worst arc voltage candidate, not only because it does not account the variability of the arc

Fig. 14. Circuit model for the analysis of arc conducted effects

Fig. 15. Time behaviour, in the initial part of the event measured and approximated

Fig. 16. Time behavior of the simulated arc voltage

Fig. 17. Time behavior of the rectangular and the simulated arc voltage at the pantograph
resistance when length changes (see Fig. 17), but also because the resulting pantograph voltage is quite different from the experimental one, as shown in Fig. 19. In the circuit model the arc is represented with a generator, whose resistance is in general negligible as shown in Fig. 14 of [18], where values of 10 to 100 mΩ are reported. In our case the observed values are of the same order (see Table I where the estimated resistance values range between 0.2 and 0.5 Ω).

V. SENSITIVITY

A sensitivity analysis was carried out for the OHL resistance \( R_{\text{OHL-DC}} \) and for \( L_{\text{filt}} \). Considering the relatively high-frequency energy content of the analyzed phenomena, the skin effect can considerably increase the OHL resistance. In order to estimate these effects, an accurate FEM (Finite Element Method) simulation was carried out for the running rails as shown in Fig. 20. The same figure also provides a visible qualitative impact of the skin effect by comparing side by side the magnetic induction field in the material at two different frequencies of the applied current: 50 Hz and 2 kHz. Results are in substantial agreement with those in [19]. The resulting skin effect makes the longitudinal resistance much larger for the frequency values characterizing the arc phenomena.

The effect of the traction line resistance on the estimated voltage waveform at the output of the measuring chain is provided in Fig. 18(a) where the estimated pantograph voltage was calculated for the following value of \( R_{\text{OHL-DC}} \): 0.17 mΩ/m, 1 mΩ/m and 3 mΩ/m.

The effect on the simulated measurement chain output of the filter inductance \( L_{\text{filt}} \) was calculated for 10 mH, 20 mH and 30 mH. The results are provided in Fig. 18(b). In particular, for lower values of the filter inductance the damping effect increases. Additionally, the oscillation frequency is slightly reduced for higher inductance values.

VI. CONCLUSIONS

A tool for the estimation of the conducted effects produced by pantograph-to-OHL arc events on the DC railway system has been developed and validated. The tool includes a complete model of the measurement chain which allows its testing with the on-board collected electrical data.

Thanks to the knowledge on the arc phenomena got from the laboratory experiments and the available measurements of the voltage and current at the pantograph, the arc voltage profile associated with a real detected event has been deduced and provided as input to the model. The comparison between pantograph voltage simulation and on-board recorded measurements is found in good agreement, whereas it is
unsatisfactory in the case of simplified rectangular arc voltage profile of the same amplitude.

The analysis on the overall line resistance (OHL+track) variation on the model output shows a limited effect. Being complex the estimate of the skin effect in transient conditions, this result provides robustness to the model.

The tool will be used in the study of conducted arc effects along the supply line, for different position of the train and different locomotives. It will then play an important role in the development of arc event detectors that exploit the on-board voltage-current measuring systems generally used for power and energy measurements. Moreover, it will be used to investigate the accuracy of the devices (measurement systems and identification algorithm) for the arc event detection.

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