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ORIGINAL PAPER

Towards a traceable divider for composite voltage waveforms below 1 kV

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Abstract

In the framework of the European Project 19NRM07 HV-com^2 supporting the standardization in high-voltage testing with composite and combined wave shapes, a divider to employ in a test set-up for validation of electrical devices submitted to composite voltages below 1 kV has been developed at the Istituto Nazionale di Ricerca Metrologica (INRIM) and currently is under extensive testing. After a simulation stage, an available divider has been modified to comply with the IEC 60,060 requirements in terms of step response and scale factor. To be suitably fast in replying to step voltages, an adjustment of the components of the low-voltage arm has been made. The divider has been calibrated with traceability to the relevant INRIM National Standards and characterized exploiting its scale factor at different voltages and frequencies. The divider has been then inserted in a set-up with a sinusoidal generator, an impulse generator and coupling–blocking elements to carry out tests at low voltages (below 1 kV) with single voltages. In these tests, the divider showed a satisfactory attitude as converting device and its scale factor is traceable with suitable uncertainty.

Keywords Voltage divider · Composite and combined voltages · Traceability · Scale factor calibration · Step response · Measurement uncertainty

1 Introduction, state of the art

Recently, the increase in electricity generation from renewable sources has changed the management of the high-voltage grid with the need to verify that the devices connected to the network are suitable for this change. For this reason, it is important that all the equipment of the network meets the requirements of the relevant standards as [1]. Therefore, the grid elements must be submitted to tests as the application of composite and combined wave shapes to verify whether they withstand the electrical phenomena to which they are submitted according to the product standards and general requirements for high-voltage measurements [2, 3].

For example, transformers, gas-insulated systems or high-voltage cables are frequently submitted to composite or combined wave shapes so the tests to which they are submitted usually consist in the application of lightning (LI) or switching (SI) impulses superimposed to high AC or DC voltages (HVAC and HVDC). Unfortunately, there is a lack in the relevant normative as it considers measurement systems and voltage dividers of test laboratories suitable for composite and combined voltages by calibrating them vs. these voltages separately. As these shapes presumably interfere each other, this calibration rule by the current normative does not give confidence that the systems and dividers are correct references if submitted to such voltages simultaneously. This could be an incorrect traceability of the wave shapes leading to possible incorrect test results. As currently, there are no references and no calibration services for composite and combined wave shapes, their resultants have to be investigated to obtain traceable and reproducible measurement set-ups to validate electrical devices when submitted to these shapes. For this reason, the Project 19NRM07 HV-com^2 has been established asking to European National Metrology Institutes (NMIs) to investigate the problems concerning the traceability and reproducibility of the measurements in

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these tests, thus supporting and reviewing the current normative to standardize the same tests. In [1–4], the definitions of combined and composite voltages with respect to the device to which they are applied and a description of the main waveforms and test set-ups for both of them are given. The project implies also the development of a test circuit for combined and composite waveforms at voltages lower than 1 kV for a simplified study of the problem. At INRIM, as partner of the project, the attention has been paid on this last task focusing on tests with composite voltages. An aim of the European project is "*New reference voltage dividers for superimposed voltages will be designed and set up*". A task is "*a modular universal voltage divider* (*a traceable reference system*) *will be designed and built for use in the calibration of the measurement systems that have been designed for measuring composite and combined waveforms*". Such a divider is not currently available. As part of this task, the peculiarity of our work has been the prototyping of a divider suitable for measurements of composite waveforms aboard a device under test reproducing at best the working conditions of such devices or the conditions under which they are submitted in the tests for their validation. The phenomenon and the influence of the elements of the test set-up on the measurement have been studied. At this stage, a low-voltage set-up has been used as suggested by the European project to perform preliminary tests and research. The traceability of the scale factor of the divider vs. National Standards has been also verified and exploited. These studies will be useful to extend the research to a full-scale divider, capable to divide properly DC, AC, LI an SI simultaneously. The work consisted first in the study of the problem through simulation and then in the choice of a divider to modify to comply with the required characteristics for the impulse test. In this paper, the attention has been paid to the set-up of the divider and in its calibration in terms of step response and of scale factor measurement.

2 The INRIM divider

Voltage dividers have played and still play a strategic role in metrology for low and high DC [5–14], AC [15–18] and impulse voltages [19–21] At INRIM, a test set-up involving a divider with a sinusoidal and a LI generators has been simulated with the LT-spice program. Simulations with single generators (LI and sinusoidal) and with composite voltages have been carried out. After this stage, a resistive–capacitive divider (compensated voltage divider), available at the INRIM High Voltage and High Power Laboratory (LATFC), has been selected to be modified to comply with the requirements of [2] in terms of step response and scale factor and to employ it in a test set-up with composite voltages. This work followed
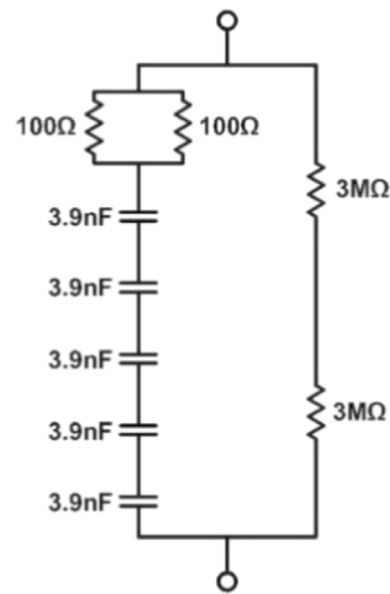

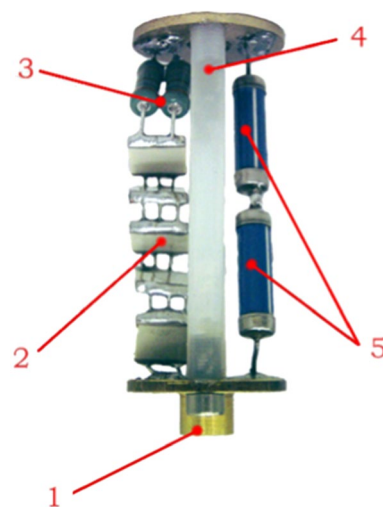**Fig. 1** INRIM divider: scheme of the high-voltage arm

Fig. 2 Divider high-voltage arm: 1. connection for the low arm; 2. ceramic capacitors; 3. RC side resistors; 4. insulating column; 5. resistive side resistors

another resistive–capacitive divider realization for medium voltages at INRIM [22]. Figures 1, 2, 3 show, respectively, the scheme of the high-voltage arm and the internal photographs of the high- and low-voltage arms of the original divider. Figure 4 shows instead the scheme of the low-voltage arm. The resistors on the capacitive side regulate the dynamic behaviour of the high-voltage arm, as their values affect the time constant of the *RC* circuit. As shown in Fig. 1 the total resistance is $R_{AT} = 6$ MΩ, while the nominal capacitance is $C_{AT} = 780$ pF.
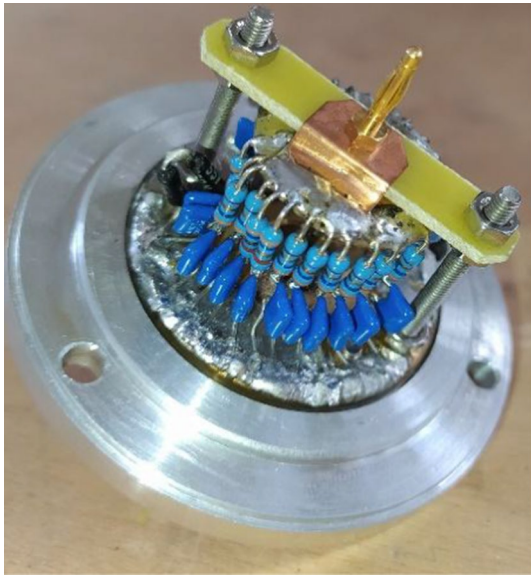
Fig. 3 INRIM divider: photograph of the low-voltage arm of the original divider performing the ratio 200. It can be replaced to obtain different ratios. At the ends, two metal discs form the short circuit to put all devices in parallel
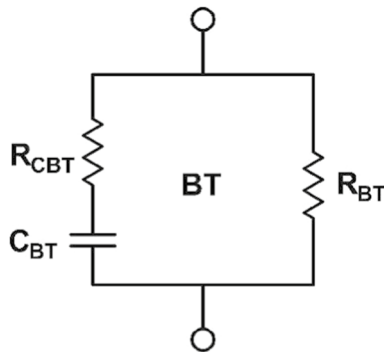

Fig. 4 Scheme of the low-voltage arm of the original divider with concentrated parameters. It consists in a resistor $R_{BT} = 30.15$ kΩ, a resistance network forming $R_{CBT} = 0.2287$ Ω and a capacitance network forming $C_{BT} = 152.2$ nF

3 Calibration of the divider

As suggested in [3] the divider has to be calibrated with an alternative method consisting in the step response tests and in the scale factor calibration.

3.1 Step response tests

With the step response tests, it is possible to evaluate the dynamic behaviour of the reference measuring systems to
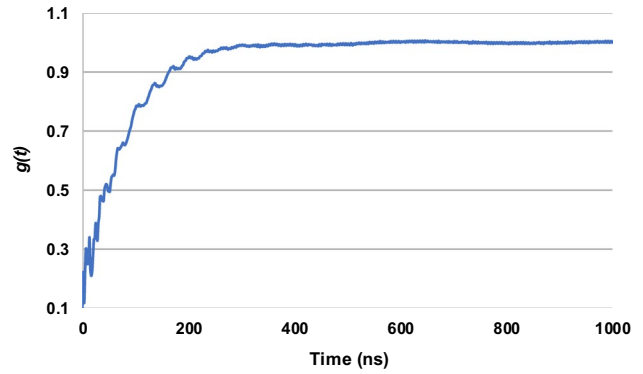

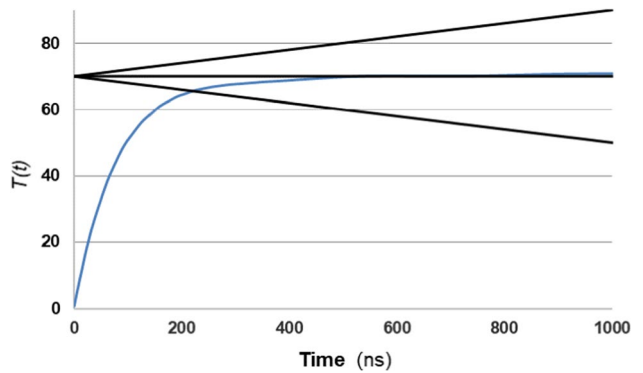**Fig. 5** Step response of the original divider

Fig. 6 Integral response of the original divider

**Table 1** Response parameters to the step voltage of the original INRIM divider

Parameter	T_N	t_s	β	T_α
Obtained	70.05 ns	220 ns	0.6717%	70.15 ns
Recommended	≤ 15 ns	≤ 200 ns		≤ 30 ns

the higher equivalent frequency of lighting impulse, validating the divider for this kind of waveforms. The first test was carried out with a step generator, which provides the required waveform by means of a mercury switch avoiding voltage bounce effects of the switch contacts. Since the step generator works better in closing due to the presence of a mercury relay, the step has been made going down. A LabVIEW program was written to analyse the divider step response. The normalized response to the step $g(t)$ and the integral step response, as defined in [3], of the original divider are shown, respectively, in Figs. 5 and 6.

Comparing to the requirements in [3], a "slow" response of the divider is observed. In fact, it takes more than 200 ns to reach the regimen. Such a delay did

**Table 2** Response parameters to the step voltage after the third change

Parameter	T_N	t_s	β	T_α
Obtained	27.25 ns	161 ns	0.7431%	25.71 ns
Recommended	≤ 15 ns	≤ 200 ns		≤ 30 ns
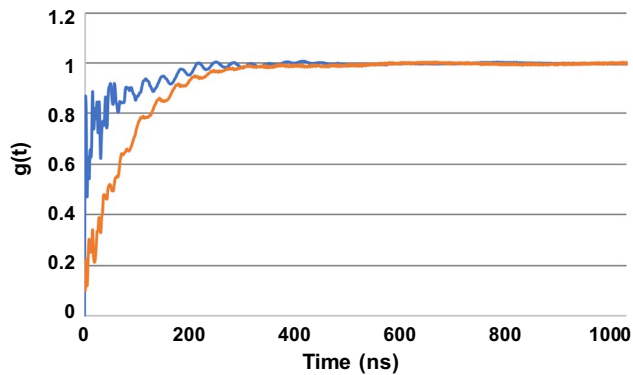
Fig. 7 Divider step response after the third change. In orange and blue, respectively, the behaviour of $g(t)$ before and after the changes on the divider
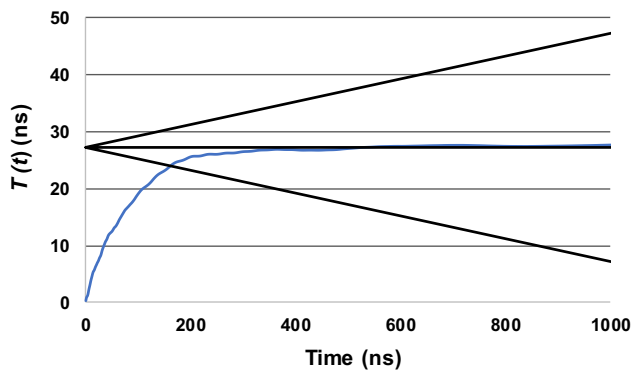
Fig. 8 Divider integral response after the third change

not represent correctly the measured impulse effect. In Table 1, the response parameters of the original divider are listed.

Here T_N and t_s are, respectively, the experimental and settling times [3]. As a consequence, the divider has been modified in successive steps adjusting its low-voltage arm checking its new performances in step response. The changes concerned only the resistors in series with the capacitors. Table 2 and Figs. 7 and 8 show, respectively, the parameters and the responses after the final change.

The oscillations in the wave front are probably due to the connection of the divider at the test set-up without a damper. In a full-scale divider, the study of the damper is mandatory
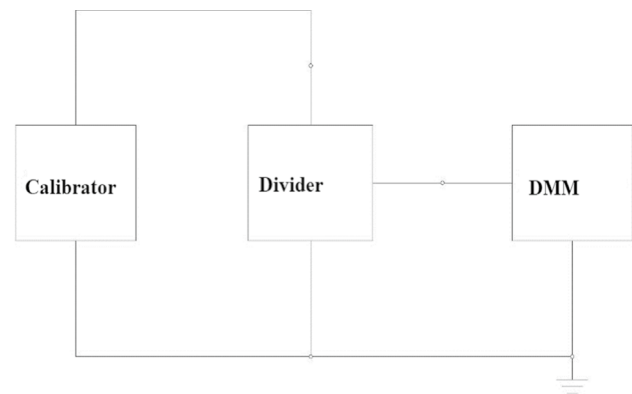
Fig. 9 Scheme of the measurement set-up for the scale factor measurement. The calibrator supplies the divider terminals while the DMM measures the voltage of the low-voltage side of the divider

but at this preliminary stage, the improvement of a damped connection has not been investigated due to the small size of the divider (and of its low resistance value) in comparison with the test set-up. It should be necessary putting a damper with a resistance value higher than that of the divider itself changing the divider ratio so impairing the measurement. In addition, for the purpose of this work, a greater bandwidth does not change the results of the measurements and the preliminary evaluations on the composite waveforms. A better bandwidth will be achieved for the full-scale divider.

In Fig. 7, it can be observed the comparison of the function $g(t)$ before and after the change. After the change, the divider has a faster response than the original version, with improvement to transient phenomena detection. Table 2 shows that two of the three parameters are satisfied, t_s and T_α, while T_N is still higher than the recommended value. Despite this, it was decided not to make further changes as our aim has been not to realize a reference divider, but a device with a satisfactory step response to involve in an experimental test circuit.

3.2 Measurement of the scale factor of the divider

According to [3], the scale factor F of a conversion device is the factor that, multiplied by the output voltage of the device, gives the input voltage to be measured. The scale factor of a measurement system is determined through a calibration usually by comparison with a reference measurement system or as the product of the scale factors of its components. Repeating its evaluation at different voltages, the linearity of the scale factor is obtained. The scale factor F is obtained as mean value of all the scale factors at different voltages. The scale factor calibration of the modified divider has been made by means a voltage ratio method with the measurement set-up of Fig. 9 in both DC and AC voltage from 20 Hz to 200 kHz. For the measurement, a J. Fluke 5502E calibrator and a precision digital Multimeter (DMM) HP 34401A were
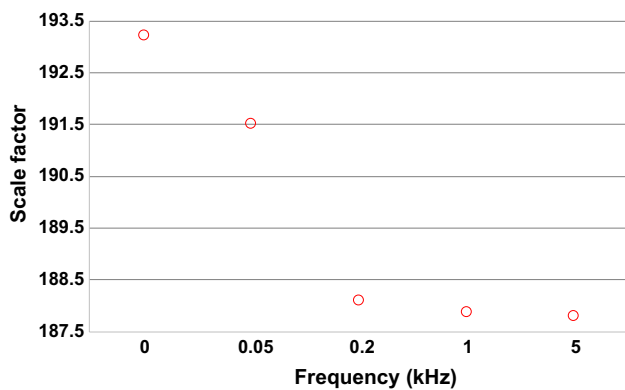
Fig. 10 Dependency vs. frequency of the scale factor of the INRIM divider
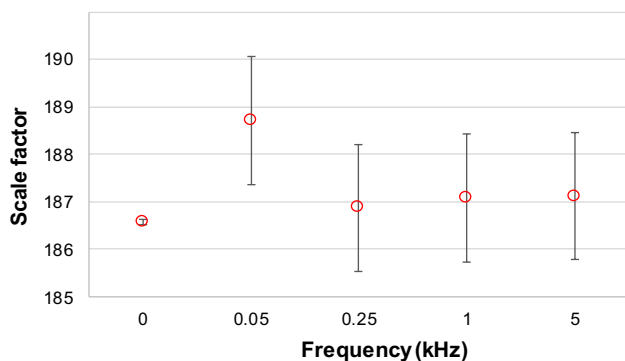

Fig. 11 Dependency vs. frequency of the scale factor of the INRIM divider after last change. The error bars correspond to the expanded uncertainties at 2σ confidence level [23]

used, respectively, to supply the voltage and to measure the voltage at the output of the divider. In Fig. 10, the scale factor value at different frequencies is reported.

The obtained scale factor F has been 189.7. The mostly different value from the others has been detected at DC voltage (193.2) with a deviation from F of 1.85% higher than the required value (1%) by the standards for the use in composite voltages (i.e. at several frequencies) [2]. The divider has been therefore further modified to improve its frequency response. Since the largest deviation occurred in DC voltage, the resistive side of the low-voltage arm of the divider has been modified. The low side resistance before the change was $R_{BT} = 31.317$ kΩ, while the high-voltage resistance has been $R_{AT} = 6$ MΩ. The desired scale factor, including the frequency up to 5 kHz, has been $F = 188$. Being F for DC voltage:

$$F = \frac{R_{AT} + R_{BT2}}{R_{BT2}} \tag{1}$$

$$R_{BT2} = \frac{R_{AT}}{F - 1} = 32.12 k\Omega \tag{2}$$

$$\Delta R = R_{BT2} - R_{BT} \cong 800\Omega \tag{3}$$

R_{BT} had to be increased of 800 Ω. After the change, it has been verified that the step response has been not significantly modified. A new calibration of the scale factor has been then performed whose results are shown in Fig. 11. The value that differed most from the others has been detected at 50 Hz (188.72), but its deviation from $F = 187.5$ has been 0.68%.

To complete the calibration, the scale factor has been measured in a wide frequency range for each voltage. In Fig. 12, the behaviour of the scale factor vs. voltage is shown.
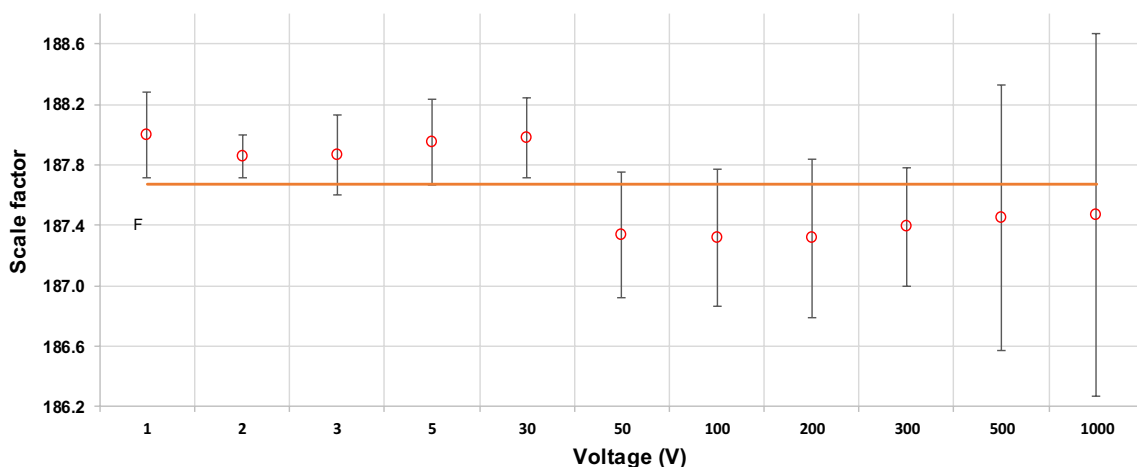

Fig. 12 Dependency of the scale factor of the INRIM divider vs. voltage after last change. In this figure, each point is the mean of the scale factors evaluated at DC and at the frequencies of 50 Hz, 75 Hz, 100 Hz, 200 Hz, 500 Hz, 1 kHz, 2 kHz, 5 kHz, 10 kHz, 20 kHz, 50 kHz, 100 kHz and 200 kHz. The error bars correspond to the expanded uncertainties at 2σ confidence level
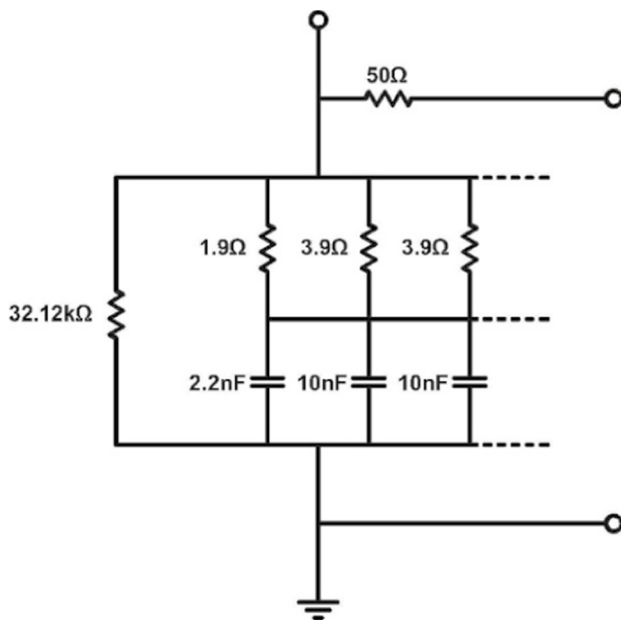
Fig. 13 Scheme of the final divider low-voltage arm. It consists in a resistor $R_{BT} = 32.12$ kΩ, a resistance network forming $R_{CBT} = 0.388$ Ω and a capacitance network forming $C_{BT} = 152.2$ nF

The scale factor has been considered almost constant vs. voltage and frequency since all the variations have been within the acceptable 1% limit. In Figs. 13 and 14, the scheme of the low-voltage arm and a photograph of the final version of the divider are shown.

3.3 Calibration uncertainties

As one aim of European Project 19NRM07 HV-com^2 is also "*the determination of the uncertainty of the existing voltage dividers and measurement systems*", examples of uncertainty evaluation, according to [23], of the calibration of the divider scale factor in two cases are given: one for DC voltage and the other for AC voltage. The measurement model can be written as:

$$F = \frac{V_{\text{cal\_acc}} + V_{\text{cal\_cal}}}{V_{\text{DMM\_acc}} + V_{\text{DMM\_cal}}} r \tag{4}$$

where:

- $F (\cong 186)$ is the unknown scale factor of the divider;
- $V_{\text{cal\_acc}}$ is the voltage supplied by the calibrator ($\cong 1000$ V) whose standard uncertainty corresponds to the one-year accuracy specifications of the calibrator;
- $V_{\text{cal\_cal}}$ is an additive voltage ($\cong 0$ V) whose standard uncertainty is obtained from the calibration certificate of the calibrator;

Fig. 14 Photograph of the INRIM divider in its final stage

- $V_{\text{DMM\_acc}}$ is the voltage measured by the DMM ($\cong 5$ V) whose standard uncertainty corresponds to the one-year accuracy specifications of the DMM;
- $V_{\text{DMM\_cal}}$ is an additive voltage ($\cong 0$ V) whose standard uncertainty is obtained from the calibration certificate of the DMM;
- $r \cong 1$ is a corrective factor of the voltage ratio measurements whose standard uncertainty is the standard deviation of the mean of the r measurements.

The standard uncertainty of F is:

$$
u^2(F) = \left(\frac{r}{V_{\text{DMM}_{\text{acc}}} + V_{\text{DMM}_{\text{cal}}}} \right)^2 \left[u^2\left(V_{\text{cal}_{\text{acc}}}\right) + u^2\left(V_{\text{cal}_{\text{cal}}}\right) \right]
$$
$$
+ \left(\frac{r\left(V_{\text{cal}_{\text{acc}}} + V_{\text{cal}_{\text{cal}}}\right)}{-(V_{\text{DMM}_{\text{acc}}} + V_{\text{DMM}_{\text{cal}}})^2} \right)^2 \left[u^2\left(V_{\text{DMMacc}}\right) \right.
$$
$$
\left. + u^2\left(V_{\text{DMMcal}}\right) \right]^2 + \left(\frac{V_{\text{cal}_{\text{acc}}} + V_{\text{cal}_{\text{cal}}}}{V_{\text{DMM}_{\text{acc}}} + V_{\text{DMM}_{\text{cal}}}} \right)^2 u^2(r) \tag{5}
$$

That can be simplified as:

$$u^2(F) = \left(\frac{1}{5V}\right)^2 \left[u^2\left(V_{cal_{acc}}\right) + u^2\left(V_{cal_{cal}}\right)\right]$$
$$+ \left(\frac{1000V}{-5V^2}\right)^2 \left[u^2\left(V_{DMMacc}\right) + u^2\left(V_{DMMcal}\right)\right]^2 \quad (6)$$
$$+ \left(186^2 u^2(r)\right)$$

where

$$c_1 = \frac{r}{V_{DMM_{acc}} + V_{DMM_{cal}}},$$
$$c_2 = \frac{r\left(V_{cal_{acc}} + V_{cal_{cal}}\right)}{-(V_{DMM_{acc}} + V_{DMM_{cal}})^2}, \quad (7)$$
$$\text{and } c_3 = \frac{V_{cal_{acc}} + V_{cal_{cal}}}{V_{DMM_{acc}} + V_{DMM_{cal}}}$$

are the sensitivity coefficients, respectively, of V_{cal_acc}, V_{cal_cal} (c_1); V_{DMM_acc}, V_{DMM_cal} (c_2); and r (c_3).

In Tables 3 and 4, the uncertainty budgets, respectively, for the calibration of the scale factor of the divider at 1000 V in DC voltage and at 1000 V at 5 kHz in AC voltage are, respectively, given.

Table 5 Simplified budget for the calibration of the divider scale factor in DC voltage at 1000 V

Component	Type	1 δ ($\times 10^{-3}$)
Calibrator accuracy	B	6.1
Calibrator calibration	B	1.1
DMM accuracy	B	24
DMM calibration	B	1.4
Measurement noise	A	negl
Standard uncertainty (normalized ratio square sum)	0.14[c]	
Expanded uncertainty	**0.27**[d]	

Bold indicates the final uncertainty value

The treatment can be simplified by means of the following two tables.

From these uncertainty budgets, it can be observed that the greatest components are due to the instruments accuracies. Nevertheless, the components due to the measurements spread and, in particular, to the instruments calibration have not to be considered always negligible, mostly in critical measurement points for the instruments themselves and for low-metrology-grade instruments. The value of F is obtained according to [3] meaning its values for the relevant voltages.

Table 3 Uncertainty budget for the calibration of the divider scale factor in DC voltage at 1000 V

Quantity	Estimate	$u(x_i)$	Type[a]	c_i	$u_i(F)$	ν_i
V_{cal_acc}	≅1000 V	56.5 mV [24]	B	≅0.2 V^{-1}	6.1×10^{-3}	≅∞
V_{cal_cal}	≅0 V	10 mV	B	≅0.2 V^{-1}	1.1×10^{-3}	≅∞
V_{DMM_acc}	≅5.36 V	225 µV [25]	B	−186.6 V^{-1}	2.4×10^{-2}	≅∞
V_{DMM_cal}	≅0 V	13 µV	B	−186.6 V^{-1}	1.4×10^{-3}	≅∞
r	≅1	7.4×10^{-17}	A	186.6	1.4×10^{-14}	17
F (y)	186.6			$u(F)$[b]	1.3×10^{-4c}	ν_{eff}≅∞
F (y)	186.6			**$U(F)$[d]**	**2.7×10^{-4}**	k≅1.96

Bold indicates the final uncertainty value

[a]Uncertainty types: With A, those obtained with statistical methods, and with B, those obtained from prior distributions [23]

[b]Standard uncertainty corresponding to a 1σ confidence level [23]

[c]This value is obtained from the square root of the quadratic sum of the u_i (F) components, further normalized to the F value [23]

[d]Expanded uncertainty corresponding to a 2σ (95.5%) confidence level [23]

Table 4 Uncertainty budget for the calibration of the divider scale factor in AC voltage at 1000 V, 5 kHz

Quantity	Estimate	$u(x_i)$	Type	c_i	$u_i(F)$	ν_i
V_{cal_acc}	≅1000 V	0.92 V [22]	B	≅0.2 V^{-1}	9.9×10^{-2}	≅∞
V_{cal_cal}	≅0 V	35 mV	B	≅0.2 V^{-1}	3.8×10^{-3}	≅∞
V_{DMM_acc}	≅5.38 V	5.5 mV [23]	B	−186.0 V^{-1}	5.9×10^{-1}	≅∞
V_{DMM_cal}	≅0 V	27 µV	B	−186.0 V^{-1}	2.9×10^{-3}	≅∞
r	≅1	2.4×10^{-6}	A	186.0	4.5×10^{-4}	17
F (y)	186.0			$u(F)$[b]	3.2×10^{-3c}	ν_{eff}=153
F (y)	186.0			**$U(F)$[d]**	**6.4×10^{-3}**	k≅2

Bold indicates the final uncertainty value

Table 6 Simplified budget for the calibration of the divider scale factor in AC voltage at 1000 V, 5 kHz

Component	Type	1 δ ($\times 10^{-3}$)
Calibrator accuracy	B	99
Calibrator calibration	B	3.8
DMM accuracy	B	590
DMM calibration	B	29
Measurement noise	A	0.45
Standard uncertainty	3.2[c]	
Expanded uncertainty	**6.4**[d]	

Bold indicates the final uncertainty value

Its type A and type B uncertainties have to be evaluated, respectively, through the standard deviation of the mean of the measurements to evaluate F and the linearity behaviour at different voltages. From the results of Tables 3, 4, 5, 6, it can be concluded that scale factor of the INRIM divider has a use uncertainty [26], even with the addition of the uncertainty components from the evaluation of its mean value, that lies within the limit required by the standards ($\leq 1\%$). The dynamic behaviour with high-frequency voltage waveforms is already considered in the step response analysis. The low values in the time response of the divider allow to consider its uncertainty as in the frequency characterization according to the procedure in [2].

4 Divider performance

As first step, the reliability of the divider employed in test set-ups with sinusoidal or impulse voltage generators, coupling and blocking elements and a data acquisition card, had to be verified.
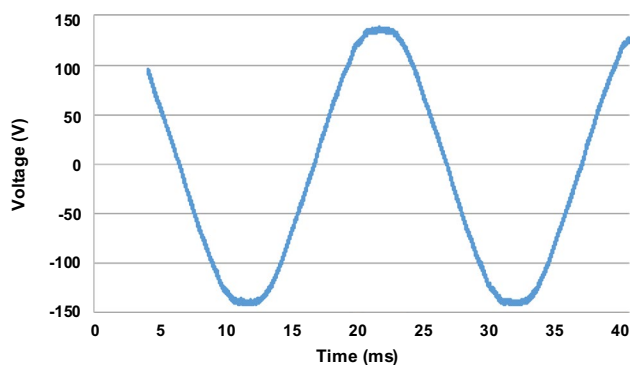

Fig. 15 Sinusoidal voltage, with RMS 100 V and 140 V magnitude applied to the divider. It correctly measures and reproduces the generated waveform
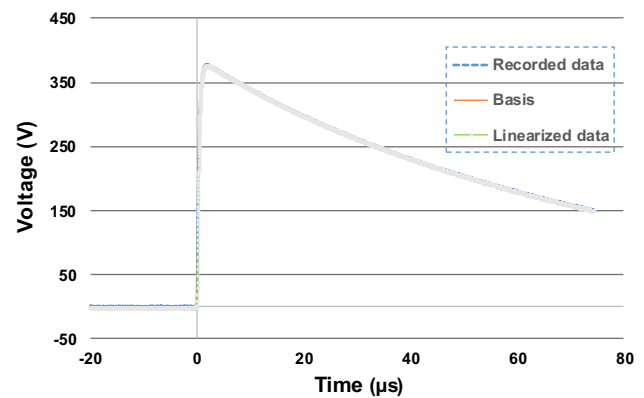

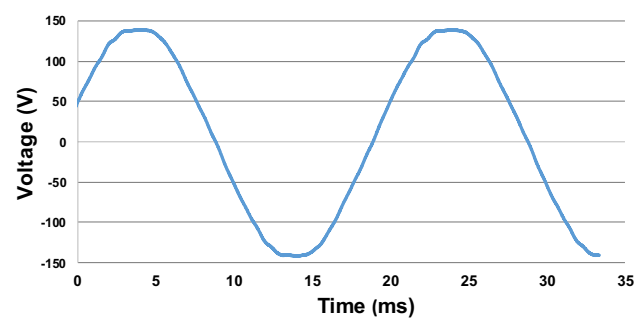**Fig. 16** LI voltage measured by the divider. Also in this case, the divider reproduces correctly the waveform

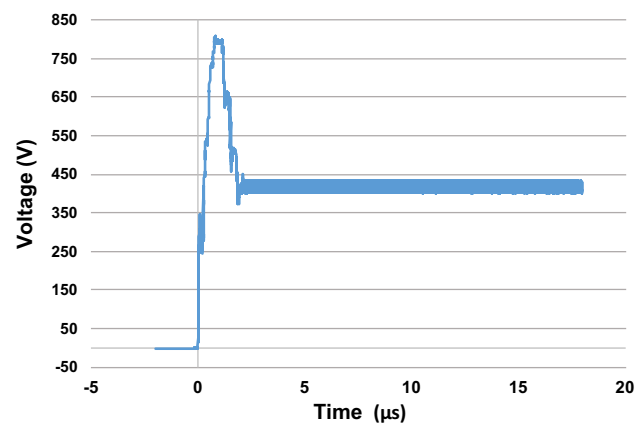**Fig. 17** Sinusoidal voltage, with RMS 100 V and 140 V magnitude applied to the divider through the 20 kΩ resistor

Fig. 18 LI voltage applied to the divider through the sphere gap. Also in this case, the divider reproduces correctly the waveform

4.1 Tests with single voltages

To develop a divider suitable for composite voltages, in a first stage the verification of the reliability of the divider

itself as converting device when submitted to single wave-forms has been made. To fulfil this task, the divider was submitted to two separate waveforms. In Fig. 15 and 16, the waveforms supplied by a sinusoidal generator and by an impulse generator, respectively, without the blocking elements measured at the output of the divider are shown.

In a second phase, the divider has been inserted in a test circuit for composite voltages [2] Sect. 9.2.3, adding a sphere gap for the impulse generator, with an additional 110 μH inductance due to the low voltage and a 20 kΩ resistor for the sinusoidal generator as blocking elements. The two converting devices of the recommended test set-up have been not inserted. The same previous tests have been repeated by alternately supplying the measurement set-up with the two generators. In Fig. 17 and 18, the waveforms measured at the output of the divider in the two situations are shown.

The block element does not modify the waveform while the divider correctly measures and reproduces the same waveform.

The voltage goes from 0 V to a peak of 800 V in a satisfactory time of a 1 μs for a LI impulse but the drop to 400 V is too fast as the standard requires a half-value time of 50 μs. In this case, the time was 2 μs due presumably to the low voltage and to the sphere gap effect.

5 Conclusion

The establishment of the European project has been due to the lack in the relevant normative concerning composite and combined waveforms and to the lack of traceable systems for these waveforms. This confirms that systems or dividers are not currently available for these shapes despite the possible test of the divider [18]. The standard developed at INRIM showed its suitability in the individual tests satisfying the required characteristics. The main difficulty in the realization of this device has been to minimize the dependency of its scale factor vs. voltage and frequency. From the detailed uncertainty budget, the scale factor of the divider is traceable to the INRIM DC and AC voltage National Standards with an overall uncertainty within 1%, satisfying the main requirements of the relevant standards. In the next future, with a set-up for composite waveforms, it will be verified whether the measurement of two waveforms separately by means of the divider and their analytical composition correctly reproduces the composite waveform on the device under test. With the same circuit, the parasitic phenomena and the noise due to the electric arc between the spheres of the spark gap will be analysed. The divider could be also used to validate the performance of the composite low-voltage generator that will be developed in the framework of the European project. The possibility of making tests with composite waveforms at low voltage with adequate accuracy will simplify the realization of a test set-up for composite waveforms at high voltages. Therefore, the divider will be useful for a complete study of combined and composite waveform quantities. A further and important aim for the future is the achievement of a better bandwidth for a full-scale divider.

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