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1           **A correction method for Vickers indenters squareness**  
2                   **measurement due to the tilt of the pyramid axis**

3  
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11                                   Abbreviated title: Vickers indenter squareness measurement correction

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25     **Abstract**

26     In ISO 6507-3 it is required that the quadrilateral base of Vickers indenter has angles of  $90^\circ \pm 0.2^\circ$ .  
27     Squareness angles are usually evaluated through optical techniques by measuring the angles between two  
28     consecutive faces, which correspond to the quadrilateral base angles when the axis of the pyramid is perfect-  
29     ly parallel to the indenter-holder axis. However, if the pyramid axis is tilted by an angle within  $0.3^\circ$ , as al-  
30     lowed by the standard, these angles no longer correspond. This work deals with the description of a numeri-  
31     cal method, based on a proper geometrical model, to correct squareness measurements. The proposed method  
32     is applied to experimental tests and measurement results, with related uncertainties, are presented. It is  
33     shown that the accuracy is improved. This method is easily implementable on different measuring systems  
34     and can be internationally adopted to improve the relevant standard.

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36  
37     **Keywords:** Hardness, Vickers indenter, squareness.

50 **1. Introduction**

51 The influence of indenter characteristics on hardness measurements, in particular for Vickers hardness, is  
52 largely reported in literature. It has been demonstrated that different indenters meeting the requirements of  
53 the Standards can lead to significantly different hardness measurements, and in particular that an increase in  
54 indenter angle entails a decrease in Vickers hardness [1,2]. It was also found that squareness errors and ridge,  
55 within the required tolerances, entail small errors in Vickers hardness [3], beyond the influence of the optical  
56 system for the evaluation of the indentation impression [4]. Also in Rockwell hardness, it was found that the  
57 main causes of differences in performance are due to imperfections in the geometric form of the indenter  
58 [5,6], and in particular that an increasing angle of the indenter entails an increase in hardness value [7]. Other  
59 works showed that hardness measurements can be affected by the roughness or mechanical deformations of  
60 the indenter under load [8] or by form errors of the indenter [9], in Rockwell C, or by friction between the  
61 indenter and material for Berkovich and cubic indenters, in microindentation hardness [10].

62 ISO 6507-3 [11] specifies the requirements of the diamond pyramidal indenter used for the calibration of  
63 hardness reference blocks. They are composed of a highly polished square-based diamond pyramid with an  
64 angle between the opposite faces of the vertex of  $136^\circ \pm 0.1^\circ$ , placed upon a steel indenter-holder, as shown  
65 in Fig. 1.

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68 **Fig. 1.** 3-D model (left) and picture (right) of a typical Vickers indenter.

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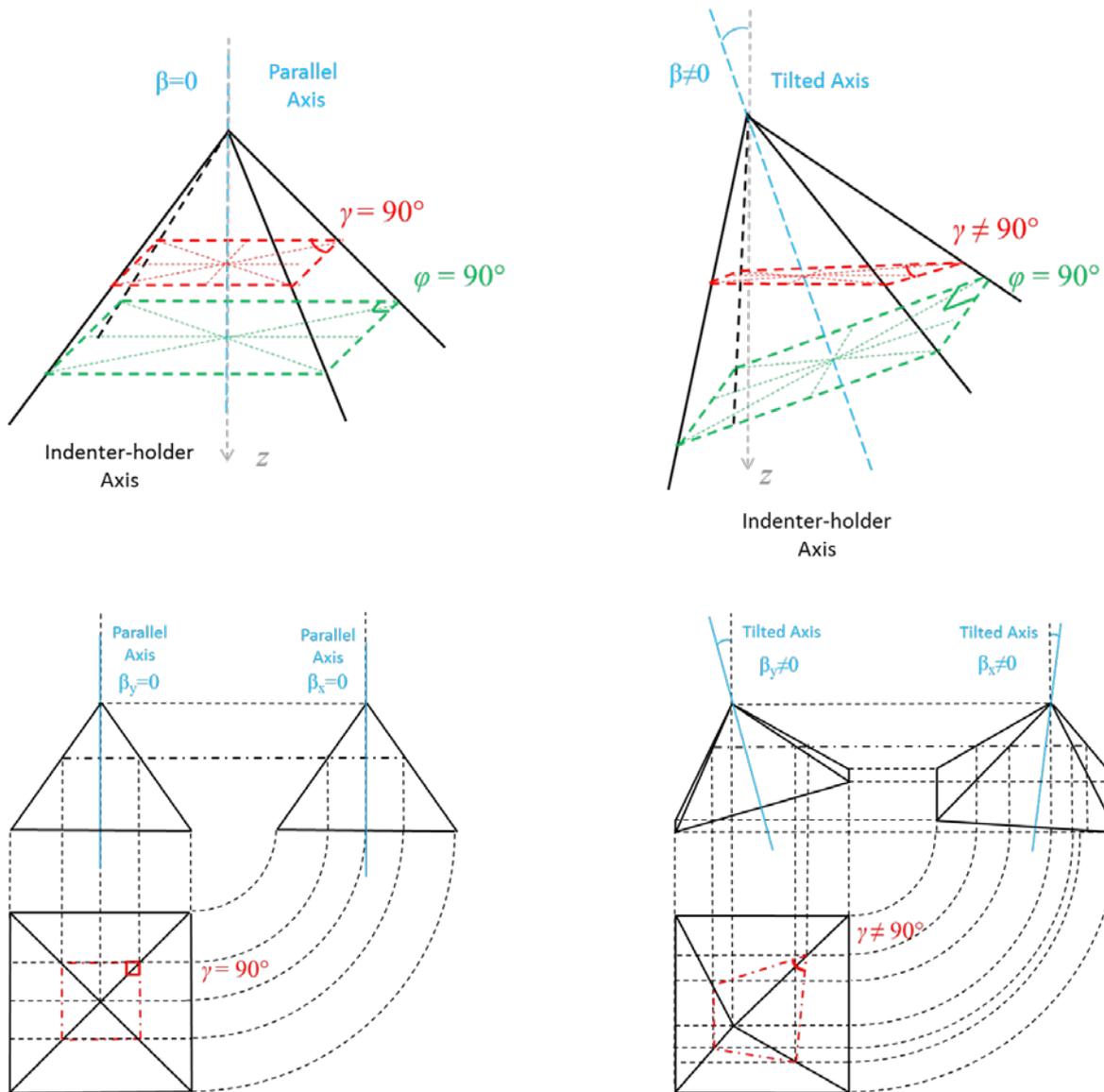
70 The pyramid quadrilateral base, which is given by the intersection of the faces with a plane perpendicular  
71 to the axis of the diamond pyramid, should have angles of  $90^\circ \pm 0.2^\circ$ . These angles are usually evaluated by

72 measuring the angles  $\gamma_{\text{exp},i=1,2,3,4}$  between two consecutive faces, assuming the indenter-holder axis as refer-  
73 ence [12,13]. Furthermore, the angle between the pyramid axis and the indenter-holder axis (normal to the  
74 seating surface), which represents the tilt angle of the pyramid axis, should be less than  $0.3^\circ$ . Nevertheless,  
75 the effect of this tilt on the measurement of the quadrilateral base angles, namely squareness measurement, is  
76 not considered in the current international standard. As a matter of fact, when the pyramid axis and indenter-  
77 holder axis, normal to the seating surface, are not parallel, the angles  $\gamma_{\text{exp},i}$  between two consecutive faces are  
78 different from the quadrilateral base angles  $\varphi_{i=1,2,3,4}$ . Such behavior affects the accuracy of squareness meas-  
79 urement, thus a correction is needed. In this work, a correction method, derived from a proper geometrical  
80 model, is proposed and described in the following Sections.

## 81 2. Measurement of Vickers indenters geometry

82 ISO 6507-3 (Sec. 5.5) requires that the indenter meets some geometrical requirements [11]. These meas-  
83 urements are usually performed in calibration laboratories by means of optical measuring systems [12-20]. In  
84 particular, the measurement of the four quadrilateral base angles  $\varphi_i$  is performed with microscopes that use  
85 angular encoders [21] or with scanning confocal chromatic probes [13]. Both methods use the indenter-  
86 holder axis or seating holder as reference. In this condition, measured angles  $\gamma_{\text{exp},i}$  correspond to the actual  
87 quadrilateral base angles  $\varphi_i$  when the axis of the pyramid is parallel to the indenter-holder axis, i.e. when it is  
88 perpendicular to the seating surface plane. However, these angles are not the same when the pyramid axis is  
89 tilted by an angle  $\beta$ , as shown in Fig. 2.

90



**Fig. 2.** Representation of a generic pyramid with a parallel axis (left) and a tilted axis (right) with respect to the indenter-holder axis, in cabinet perspective (top) and in orthogonal projection (bottom). The actual square-base angles are depicted in green and the measured angles between two consecutive faces are depicted in red.

By way of example, in INRiM hardness laboratory, the Galileo-LTF® Gal-Indent optical system is adopted (Fig. 3) [12]. This system is able to measure the two vertex angles  $\alpha_x$  and  $\alpha_y$  of the indenter (nominally  $136^\circ$ ) along  $x$ - and  $y$ -axis, respectively, between two opposite faces, and the four angles  $\gamma_{exp,i}$  between two consecutive faces (nominally  $90^\circ$ ) by means of two angular encoders mounted on the optical measuring system [21].

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**Fig. 3.** The Galileo-LTF® Gal-Indent optical system used at INRiM hardness laboratory for the measurement of the vertex angles and the quadrilateral base angles.

Its geometrical characteristics assure that all mechanical parts are perfectly aligned and that the Vickers indenter-holder axis is perpendicular to the lens of the system. The optical system is based on Mirau interferometry, where a light beam (wavelength of 546 nm) is split into two beams: one is reflected to the observer (either through the eyepieces or through a TV Camera), the other hits a Vickers indenter lateral face and is reflected to the observer as well. The two beams recombine and generate an interference pattern. The indenter is simultaneously rotated around the axis passing through the pyramid vertex normal to the plane containing the indenter-holder axis and the optical lens axis, and around the indenter-holder axis, until a lateral face is parallel to the plane of the microscope lens by observing the interference fringes. These two rotations are measured by means of two angular encoders. Rotations around the indenter-holder axis represent the meas-

116 urement of the angles  $\gamma_{\text{exp},i}$  between two consecutive faces, whereas, for each lateral face, rotations around  
 117 the axis passing through the pyramid vertex normal to the plane containing the indenter-holder axis and the  
 118 optical lens axis represent the measurement of the supplementary angles  $(\omega_{x-}, \omega_{x+}, \omega_{y-}, \omega_{y+})$  along  $x$ - and  $y$ -  
 119 axis in clockwise (-) and counter clockwise (+) directions, according to Fig. 4. In this way, the two vertex  
 120 angles  $\alpha_x$  and  $\alpha_y$  and the pyramid tilt angles  $\beta_x$  and  $\beta_y$ , along  $x$ - and  $y$ - axis, can be calculated, respectively,  
 121 according to Eqs. (1) and Eqs. (2). By way of example, in Fig. 4, the cross-section of a Vickers indenter  
 122 through  $yz$  plane shows the measured vertex angle  $\alpha_y$  and the tilt angle  $\beta_y$ .

123 By decomposing the pyramid tilted axis vector  $\mathbf{v}$  along  $xz$  and  $yz$  planes, according to Fig. 5, Eq. (3) and  
 124 Eq. (4) can be derived and combined. From Eq. (4), it is then possible to derive the relationship between the  
 125 total tilt angle  $\beta$  and the pyramid tilt angles  $\beta_x$  and  $\beta_y$ , along  $x$ - and  $y$ - axis, as shown in Eq. (5), which, in  
 126 turn, can be approximated to Eq. (6) by applying small-angle approximation as the angle between the pyra-  
 127 mid axis and the indenter-holder axis is in the order of  $10^{-1}^\circ$ .

128

$$\alpha_x = 180 - (\omega_{x+} + \omega_{x-}); \quad \alpha_y = 180 - (\omega_{y+} + \omega_{y-}) \quad (1)$$

129

$$\beta_x = \frac{\omega_{x+} - \omega_{x-}}{2}; \quad \beta_y = \frac{\omega_{y+} - \omega_{y-}}{2} \quad (2)$$

130

$$\|\mathbf{v}\| \cos \beta = \|\mathbf{v}_{xz}\| \cos \beta_x = \|\mathbf{v}_{yz}\| \cos \beta_y \quad (3)$$

131

$$\begin{aligned} \|\mathbf{v}\| \sin \beta &= \sqrt{(\|\mathbf{v}_{xz}\| \sin \beta_x)^2 + (\|\mathbf{v}_{yz}\| \sin \beta_y)^2} = \\ &= \sqrt{\left(\frac{\|\mathbf{v}\| \cos \beta}{\cos \beta_x} \sin \beta_x\right)^2 + \left(\frac{\|\mathbf{v}\| \cos \beta}{\cos \beta_y} \sin \beta_y\right)^2} = \|\mathbf{v}\| \cos \beta \sqrt{\left(\frac{\sin \beta_x}{\cos \beta_x}\right)^2 + \left(\frac{\sin \beta_y}{\cos \beta_y}\right)^2} \end{aligned} \quad (4)$$

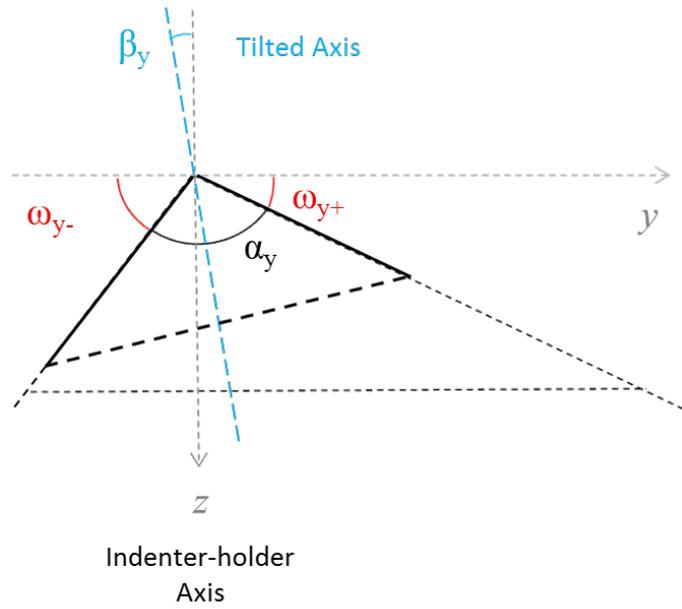
132

$$\tan \beta = \sqrt{(\tan \beta_x)^2 + (\tan \beta_y)^2} \quad (5)$$

133

$$\beta = \sqrt{\beta_x^2 + \beta_y^2} \quad (6)$$

134

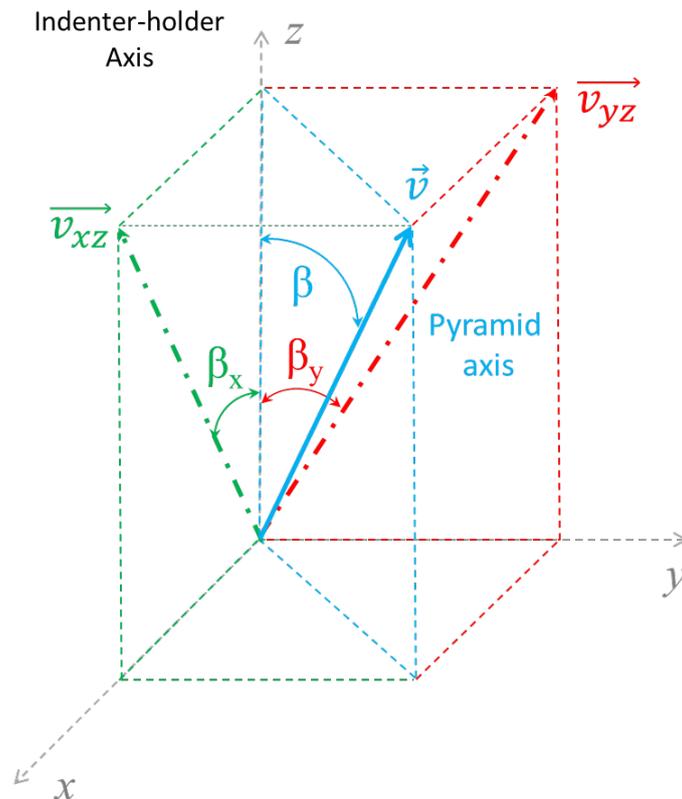


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136

**Fig. 4.** Cross-section of Vickers indenter angles measured with the optical system through yz plane.

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**Fig. 5.** Decomposition of the tilted pyramid axis vector  $\vec{v}$  and the associated angles along x- and y- axis.

140

141 **3. Correction method**

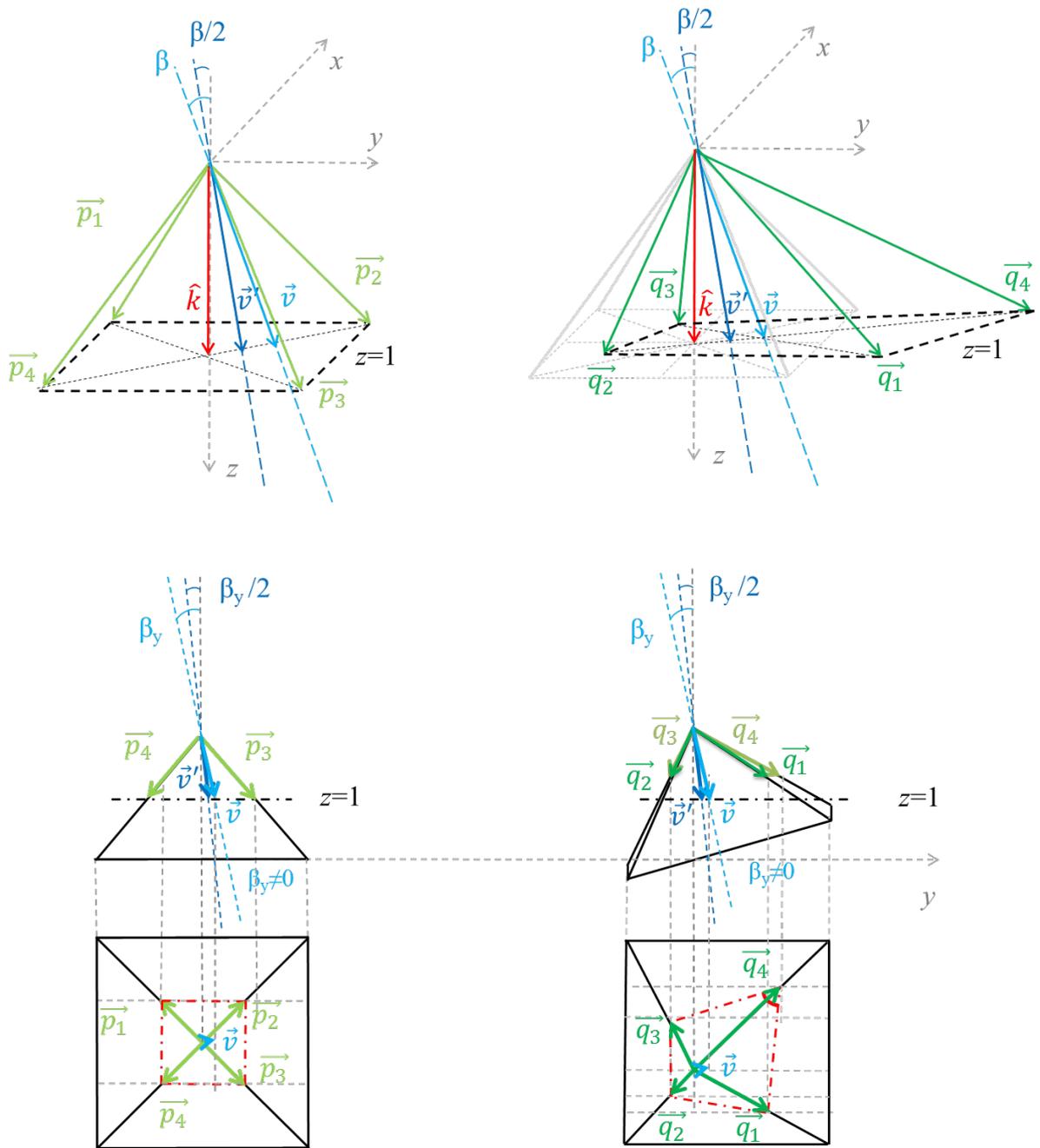
142 The geometrical model at the base of the correction method aims to calculate the theoretical angles  $\gamma_i$  of  
 143 an ideal square-based pyramid with a tilted axis with respect to the indenter-holder axis, and correct the  
 144 measured quadrilateral base angles  $\gamma_{exp,i}$ . The following equations are based on fundamental elements of  
 145 linear algebra [22].

146 Firstly, by cutting the tilted pyramid with a horizontal plane ( $z = 1$ ) perpendicular to the indenter-holder  
 147 axis unit vector  $\mathbf{k} = (0,0,1)$ , the vectors  $\mathbf{v}'$  and  $\mathbf{p}_{i=1,2,3,4}$ , which represent the vectors of the bisector between  
 148 the indenter-holder axis  $\mathbf{k}$  and the pyramid axis  $\mathbf{v}$ , and the four lateral edges of the associated right pyramid,  
 149 respectively, are defined according to Eqs. (7). Vectors are shown in Fig. 6 (left) and Fig. 7 (top-left). The  
 150 bisector between the indenter-holder axis  $\mathbf{k}$  and the pyramid axis  $\mathbf{v}$  is used to perform the rotation of the lat-  
 151 eral edge vectors  $\mathbf{p}_i$  by finding its symmetrical vectors  $\mathbf{q}_i$ , as described below.

152

$$\left\{ \begin{array}{l} \mathbf{v}' = (v'_x, v'_y, v'_z) = \left( \tan \frac{\beta_x}{2}, \tan \frac{\beta_y}{2}, 1 \right) \\ \mathbf{p}_1 = (p_{1x}, p_{1y}, p_{1z}) = \left( \tan \frac{\alpha_x}{2}, -\tan \frac{\alpha_y}{2}, 1 \right) \\ \mathbf{p}_2 = (p_{2x}, p_{2y}, p_{2z}) = \left( \tan \frac{\alpha_x}{2}, \tan \frac{\alpha_y}{2}, 1 \right) \\ \mathbf{p}_3 = (p_{3x}, p_{3y}, p_{3z}) = \left( -\tan \frac{\alpha_x}{2}, \tan \frac{\alpha_y}{2}, 1 \right) \\ \mathbf{p}_4 = (p_{4x}, p_{4y}, p_{4z}) = \left( -\tan \frac{\alpha_x}{2}, -\tan \frac{\alpha_y}{2}, 1 \right) \end{array} \right. \quad (7)$$

153



**Fig. 6.** Vectors of the associated right pyramid (left) and the tilted pyramid (right) in cabinet perspective (top) and in orthogonal projection (bottom).

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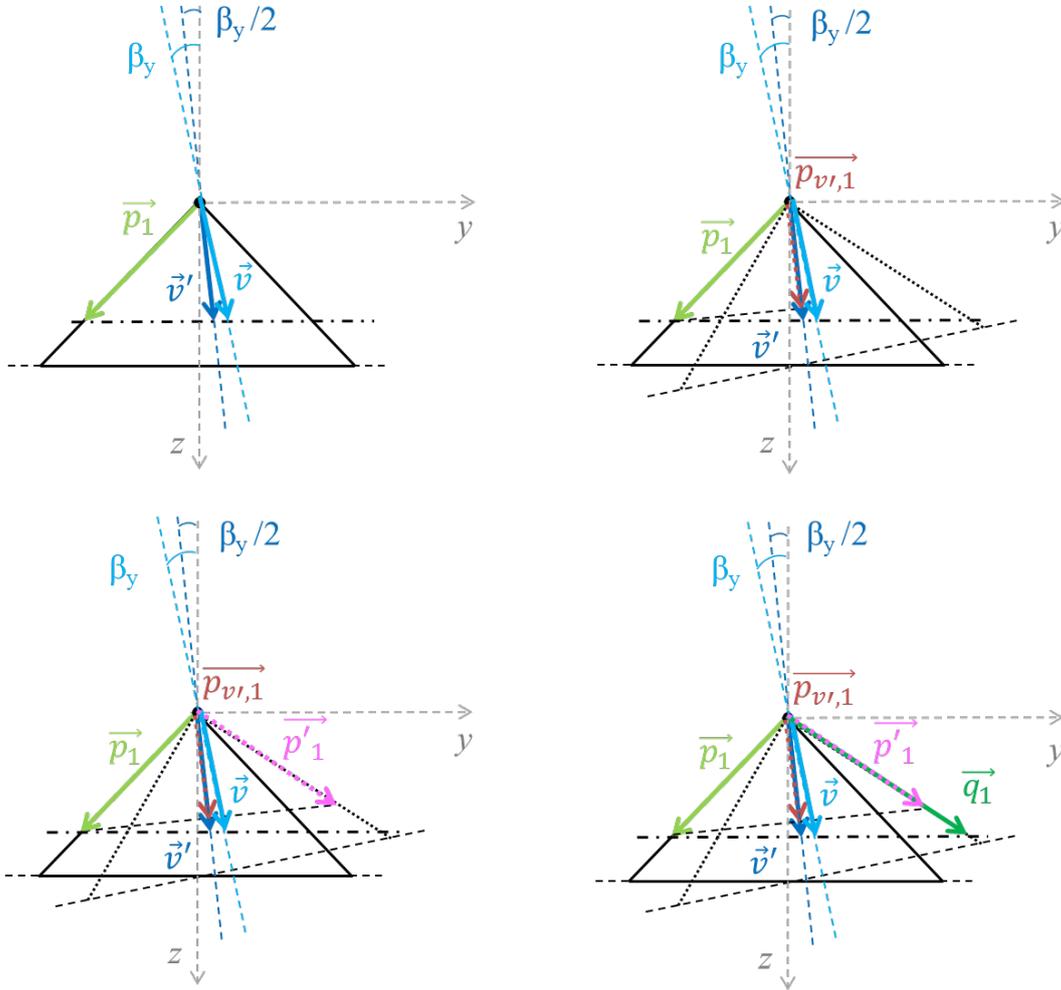
158 By tilting the pyramid by an angle  $\beta$ , the vectors  $\mathbf{p}_{v,i}$ , which represent the projection of  $\mathbf{p}_i$  on  $\mathbf{v}'$ , can be  
 159 defined according to Eq. (8) and are shown in Fig. 7 (top-right).

160

$$\mathbf{p}_{v',i} = (p_{v',ix}, p_{v',iy}, p_{v',iz}) = \tag{8}$$

$$= \left( \left( \mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|} \right) \frac{v'_x}{\|\mathbf{v}'\|}, \left( \mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|} \right) \frac{v'_y}{\|\mathbf{v}'\|}, \left( \mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|} \right) \frac{v'_z}{\|\mathbf{v}'\|} \right)$$

161



162

163

**Fig. 7.** Defined vectors (for  $i=1$ ) on the  $yz$  plane cross-section.

164

165 Considering the tip of vector  $\mathbf{p}_{v,i}$  as the midpoint, it is possible to get the lateral edge vectors  $\mathbf{p}'_i$  symmet-

166 rical to  $\mathbf{p}_i$ , according to Eq. (9), as depicted in Fig. 7 (bottom-left).

167

$$\begin{aligned} \mathbf{p}'_i &= (p'_{ix}, p'_{iy}, p'_{iz}) = (2p_{v',ix} - p_{ix}, 2p_{v',iy} - p_{iy}, 2p_{v',iz} - p_{iz}) = \\ &= \left( 2 \left( \mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|} \right) \frac{v'_x}{\|\mathbf{v}'\|} - p_{ix}, 2 \left( \mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|} \right) \frac{v'_y}{\|\mathbf{v}'\|} - p_{iy}, 2 \left( \mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|} \right) \frac{v'_z}{\|\mathbf{v}'\|} - p_{iz} \right) \end{aligned} \quad (9)$$

168 Then, by stretching the vectors  $\mathbf{p}'_i$  to the plane  $z=1$  and reminding that  $p_{iz}=1$ , it is possible to obtain the  
 169 vectors  $\mathbf{q}_i$ , which represent the lateral edge vectors of the tilted square-base pyramid, according to Eq. (10).  
 170 These vectors are represented in Fig. 6 (right) and Fig.7 (bottom-right).

171

$$\begin{aligned} \mathbf{q}_i = (q_{ix}, q_{iy}, q_{iz}) &= \left( \frac{2(\mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|}) \frac{v'_x}{\|\mathbf{v}'\|} - p_{ix}}{2(\mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|}) \frac{v'_z}{\|\mathbf{v}'\|} - p_{iz}}, \frac{2(\mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|}) \frac{v'_y}{\|\mathbf{v}'\|} - p_{iy}}{2(\mathbf{p}_i \cdot \frac{\mathbf{v}'}{\|\mathbf{v}'\|}) \frac{v'_z}{\|\mathbf{v}'\|} - p_{iz}}, 1 \right) = \\ &= \left( \frac{2(\mathbf{p}_i \cdot \mathbf{v}')v'_x - p_{ix}\|\mathbf{v}'\|^2}{2(\mathbf{p}_i \cdot \mathbf{v}')v'_z - p_{iz}\|\mathbf{v}'\|^2}, \frac{2(\mathbf{p}_i \cdot \mathbf{v}')v'_y - p_{iy}\|\mathbf{v}'\|^2}{2(\mathbf{p}_i \cdot \mathbf{v}')v'_z - p_{iz}\|\mathbf{v}'\|^2}, 1 \right) = \\ &= \left( \frac{2(\mathbf{p}_i \cdot \mathbf{v}')v'_x - p_{ix}\|\mathbf{v}'\|^2}{2(\mathbf{p}_i \cdot \mathbf{v}') - \|\mathbf{v}'\|^2}, \frac{2(\mathbf{p}_i \cdot \mathbf{v}')v'_y - p_{iy}\|\mathbf{v}'\|^2}{2(\mathbf{p}_i \cdot \mathbf{v}') - \|\mathbf{v}'\|^2}, 1 \right) \end{aligned} \quad (10)$$

172

173 By subtracting two consecutive vectors  $\mathbf{q}_i$ , the quadrilateral base vectors  $\mathbf{r}_i$  are obtained according to  
 174 Eqs. (11), and the theoretical angles  $\gamma_i$  of a tilted square-based pyramid can thus be found according to  
 175 Eqs. (12) (see Fig. 8).

176

$$\begin{cases} \mathbf{r}_{i=1,2,3} = \mathbf{q}_i - \mathbf{q}_{i+1} \\ \mathbf{r}_4 = \mathbf{q}_4 - \mathbf{q}_1 \end{cases} \quad (11)$$

177

$$\begin{cases} \gamma_{i=1,2,3} = \cos^{-1} \left( \frac{\mathbf{r}_i \cdot (-\mathbf{r}_{i+1})}{\|\mathbf{r}_i\| \cdot \|\mathbf{r}_{i+1}\|} \right) \\ \gamma_4 = 360 - \gamma_1 - \gamma_2 - \gamma_3 \end{cases} \quad (12)$$

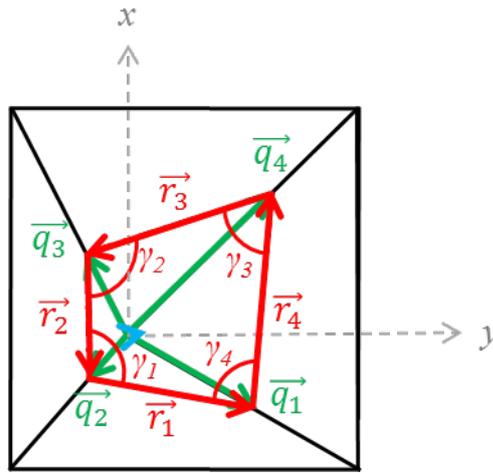


Fig. 8. Quadrilateral base vectors and angles.

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180

181 In this way, the measured angles  $\gamma_{exp,i}$  can be corrected and the actual angles  $\varphi_i$  of the quadrilateral base  
 182 of the tilted pyramid can be numerically evaluated according to Eq. (13).

183

$$\varphi_i = 90 + \gamma_{exp,i} - \gamma_i \quad (13)$$

#### 184 4. Measurement results and associated uncertainty

185 In this Section, the application of the numerical correction method to experimental squareness measure-  
 186 ments is presented. The Vickers indenter under test is a Galileo-LTF® indenter. Measurements are per-  
 187 formed at INRiM with the Galileo-LTF® Gal-Indent optical system, described in Section 2. Currently, at  
 188 international level, traceability of Vickers diamond indenter angle measurements, according to ISO 6507-3,  
 189 are guaranteed by INRiM with absolute expanded uncertainties ( $k = 2, 95\%$  of confidence level) of  $0.05^\circ$   
 190 for the tilt angle  $\beta$ , for the angles between the opposite faces of the vertex  $\alpha$  and for the angles of the quadri-  
 191 lateral base  $\gamma_{exp,i}$ .

192 In this illustrative case, the measured supplementary angles of the diamond pyramidal indenter along x-  
 193 and y- directions ( $\omega_{x+}, \omega_{x-}, \omega_{y+}, \omega_{y-}$ ) are  $21.980^\circ, 22.089^\circ, 22.131^\circ$  and  $21.955^\circ$ , respectively, and the meas-  
 194 ured squareness angles between two consecutive faces ( $\gamma_{exp,1}, \gamma_{exp,2}, \gamma_{exp,3}, \gamma_{exp,4}$ ) are  $90.11^\circ, 90.38^\circ, 89.95^\circ$   
 195 and  $89.57^\circ$ , respectively. According to Eq. (1), the measured vertex angles  $\alpha_x$  and  $\alpha_y$  of the indenter along x-

196 and y-axis are  $135.93^\circ$  and  $135.91^\circ$ , respectively. Both are within the corresponding tolerance interval ( $136^\circ$   
 197  $\pm 0.1^\circ$ ). The tilt angles  $\beta_x$  and  $\beta_y$ , evaluated according to Eq. (2), are  $-0.05^\circ$  and  $0.09^\circ$ , respectively, thus the  
 198 total tilt angle is  $0.10^\circ$ , according to Eq. (6), which is within the standard tolerance of  $0.30^\circ$ . These data are  
 199 used as inputs in the previous equations and, in this way, the theoretical angles of the associated square-base  
 200 pyramid  $\gamma_i$  can be found.

201 Squareness angles  $\gamma_{exp,i}$ , theoretical angles of the associated tilted square-base pyramid  $\gamma_i$ , and the cor-  
 202 rected angles  $\varphi_i$ , according to Eq. (13), along with the expanded uncertainties (coverage factor,  $k=2$ ) evaluat-  
 203 ed according to GUM [23], are listed in Table 1.

204 It is observed that without the correction, two angles (2 and 4) are outside the tolerance interval. The dif-  
 205 ference between corrected and measured angles ( $\varphi_i - \gamma_{exp,i}$ ) to show the magnitude of correction, and the dif-  
 206 ference between corrected angles  $\varphi_i$  and  $90^\circ$  to verify the compliance with the requirement of the relevant  
 207 standard, are also reported. It is shown that the maximum correction is  $0.35^\circ$  and that the application of the  
 208 proposed procedure allows, in this illustrative case, to fulfill the standard requirements.

209

210 **Table 1**

211 Experimental squareness measurement with the implementation of the correction method.

Angle $i$	Measured angle $\gamma_{exp,i} / ^\circ$	Theoretical angle $\gamma_i / ^\circ$	Corrected angle $\varphi_i / ^\circ$	$\varphi_i - \gamma_{exp,i} / ^\circ$	$\varphi_i - 90 / ^\circ$
1	$90.11 \pm 0.05$	$90.10 \pm 0.03$	$90.01 \pm 0.06$	$-0.10 \pm 0.06$	$0.01 \pm 0.06$
2	$90.38 \pm 0.05$	$90.34 \pm 0.03$	$90.04 \pm 0.06$	$-0.34 \pm 0.06$	$0.04 \pm 0.06$
3	$89.95 \pm 0.05$	$89.90 \pm 0.03$	$90.05 \pm 0.06$	$0.10 \pm 0.06$	$0.05 \pm 0.06$
4	$89.57 \pm 0.05$	$89.65 \pm 0.03$	$89.92 \pm 0.06$	$0.35 \pm 0.06$	$-0.08 \pm 0.06$

212

213 **5. Conclusions**

214 ISO 6507-3 specifies that the quadrilateral base of the diamond pyramidal Vickers indenter used for the  
215 calibration of hardness reference blocks has angles of  $90^\circ \pm 0.2^\circ$ . This measurement is usually performed  
216 with optical techniques by measuring the angles between two consecutive lateral faces, using the indenter-  
217 holder axis or seating holder as reference. However, if the pyramid axis is tilted by a maximum angle of  $0.3^\circ$   
218 with respect to the indenter-holder axis, as allowed by the standard, squareness measurement is not accurate  
219 enough. In fact, in this case, the actual quadrilateral base angles do not correspond to the angles between two  
220 consecutive faces. Such behavior affects the accuracy of squareness measurement, thus a correction is need-  
221 ed. In this work, a numerical correction method, derived from a proper geometrical model of the Vickers  
222 indenter, is finally proposed and described to overcome this issue. Its implementation on experimental meas-  
223 urements, reported along with the associated uncertainties, shows that the correction method improves the  
224 accuracy of Vickers indenters squareness measurement. Furthermore, since it is suitable for different measur-  
225 ing systems and is easily implementable, even on common spreadsheets, the method can be adopted interna-  
226 tionally, in the future, to improve the relevant standard. Future works will be aimed at extending the correc-  
227 tion method for Rockwell and Berkovich indenters and at evaluating more in-depth the direct influence of  
228 squareness and tilt errors on Vickers hardness tests.

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231 supporting the work and providing precious and essential suggestions.

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