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Quantum characterization of superconducting photon counters

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Abstract. We address the quantum characterization of photon counters based on transition-edge sensors (TESs) and present the first experimental tomography of the positive operator-valued measure (POVM) of a TES. We provide the reliable tomographic reconstruction of the POVM elements up to 11 detected photons and M=100 incoming photons, demonstrating that it is a linear detector.

Contents

1.	Introduction	2
2.	The positive operator-valued measurement reconstruction technique	2
3.	Experiment	3
4.	Results	5
Acknowledgments		7
Re	References	

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1. Introduction

The possibility of discriminating the number of impinging photons on a detector is a fundamental tool in many different fields of optical science and technology [1], including nanopositioning and the redefinition of candela unit in quantum metrology [2, 3], foundations of quantum mechanics [4], quantum imaging [5] and quantum information [6–9], e.g. for communication and cryptography. As a matter of fact, conventional single-photon detectors can only distinguish between zero and one (or more) detected photons, with photon number resolution that can be obtained by spatially [10] or temporally [11] multiplexing this kind of on/off detector.

Genuine photon number resolving (PNR) detectors need a process intrinsically able to produce a pulse proportional to the number of absorbed photons. In fact, detectors with PNR capability are few, e.g. photo-multiplier tubes [12], hybrid photo-detectors [13] and quantum-dot field-effect transistors [14]. At the moment, the most promising genuine PNR detectors are visible light photon counters [15] and transition edge sensors (TESs) [16–21], i.e. microcalorimeters based on a superconducting thin film working as a very sensitive thermometer [22].

For the practical application of these detectors, it is crucial to achieve their precise characterization [23–30]. In particular, it is generally assumed that TESs are linear photon counters, with a detection process corresponding to a binomial convolution. It is also expected that dark counts are not present in TESs. Taken together, these assumptions allow one to characterize a TES by a single number assessing the quantum efficiency of the detector, i.e. the probability $0 \le \eta \le 1$ that a photon impinging on the detector is actually revealed. In this paper, we present the first experimental reconstruction of the positive operator-valued measurement (POVM) describing the operation of a TES and, in turn, the first demonstration of the linearity. In section 2, we illustrate the method used for POVM reconstruction, while in section 3 we describe the experimental implementation. In section 4, we discuss the results and close the paper with some concluding remarks.

2. The positive operator-valued measurement reconstruction technique

As TESs are microcalorimeters, they are intrinsically phase-insensitive detectors. In the following, we thus assume that the elements of the POVM $\{\Pi_n\}$ are diagonal operators in the Fock basis, i.e.

$$\Pi_n = \sum_m \Pi_{nm} |m\rangle\langle m|,\tag{1}$$

with the completeness relation $\sum_n \Pi_n = \mathbf{I}$. Matrix elements $\Pi_{nm} = \langle m | \Pi_n | m \rangle$ describe the detector response to m incoming photons, i.e. the probability of detecting n photons with m photons at the input⁵. A reconstruction scheme for Π_{nm} , i.e. a tomography of the POVM, provides the characterization of the detector at the quantum level. In order to achieve the tomography of the TES POVM, we exploit an effective and statistically reliable

⁵ This corresponds to considering our TES as a *gray box* (instead of a black box), on the basis of this solid physics assumption, i.e. the fact that they are microbolometers. On the other hand, trying to find experimental evidence for this phase-insensitiveness assumption is pointless, as there is no phase reference (e.g. from the TES itself) to modify the phase of our probe states with respect to it.

technique [31–33] based on recording the detector response for a known and suitably chosen set of input states, e.g. an ensemble of coherent signals providing a sample of the Husimi *Q*-function of the elements of the POVM.

Let us consider a set of K coherent states of different amplitudes $|\alpha_j\rangle$, $j=1,\ldots,K$. The probability of obtaining the outcome n from the TES, i.e. of detecting n photons, with the jth state as input is given by

$$p_{nj} = \text{Tr}[|\alpha_j\rangle\langle\alpha_j|\Pi_n] = \sum_m \Pi_{nm} q_{mj}, \qquad (2)$$

where $q_{mj} = \exp(-\mu_j)\mu_j^m/m!$ is the ideal photon statistics of the coherent state $|\alpha_j\rangle$, $\mu_j = |\alpha_j|^2$ being the average number of photons. In order to reconstruct the matrix elements Π_{nm} , we sample the probabilities p_{nj} and invert the statistical model composed of the set of equations (2). Since the Fock space is infinite dimensional, this estimation problem contains, in principle, an infinite number of unknowns.

A suitable truncation at a certain dimension M should be performed, with the constraint that the probability of having $m \ge M$ photons in the states $|\alpha_j\rangle$ is not too large. In other words, given the set of probing coherent states, we have a small number of data for the entries with $m \ge M$ and we cannot investigate the performances of the detector above the corresponding energy regimes.

The distributions p_{nj} in equation (2) provide a sample of the Q-functions $\langle \alpha_j | \Pi_n | \alpha_j \rangle$ of the POVM elements, and any reconstruction scheme for the Π_{nm} basically amounts to recovering the Fock representation of the Π_n 's from their phase space Q-representation. In general, this cannot be done exactly due to singularity of the antinormal ordering of the Fock number projectors $|n\rangle\langle n|$ [34]. On the other hand, upon exploiting the truncation described above, we deal with POVM elements expressed as a finite mixture of Fock states, which are amenable to reconstruction [35, 36]. The statistical model in (2) may be solved using maximum likelihood (ML) methods or a suitable approximation of ML. We found that reliable results are obtained already with a least-squares fit, i.e. we have effectively estimated Π_{nm} by the minimization of a regularized version of the square difference $\sum_{nj} (\sum_{m=0}^{M-1} q_{mj} \Pi_{nm} - p_{nj})^2$, where the physical constraints of smoothness are implemented by exploiting a convex, quadratic and device-independent function [32]. We also force normalization $\sum_{n=0}^{N-1} \Pi_{nm} = 1$, $\forall m$, where the last POVM element is defined as $\Pi_{N-1} = 1 - \sum_{n=0}^{N-2} \Pi_n$.

3. Experiment

The TES we have characterized is composed of a \sim 90 nm thick Ti/Au film [37, 38], fabricated by e-beam deposition on silicon nitride substrates. The effective sensitive area, obtained by lithography and chemical etching, is $20 \times 20 \,\mu\text{m}^2$. The superconducting wirings of Al, with thicknesses between 100 and 150 nm, have been defined by a lift-off technique combined with radiofrequency sputtering of the superconducting films. Upon varying the top Ti film thickness, the critical temperatures of these TESs can range between 90 and 130 mK, showing a sharp transition (1–2 mK).

The characterization of TES has been carried out in a dilution refrigerator with a base temperature of 30 mK. Furthermore, the detector is voltage biased, in order to take advantage of the negative electro-thermal feedback, providing the possibility of obtaining a self-regulation of the bias point without a fine temperature control and reducing the detector response time.

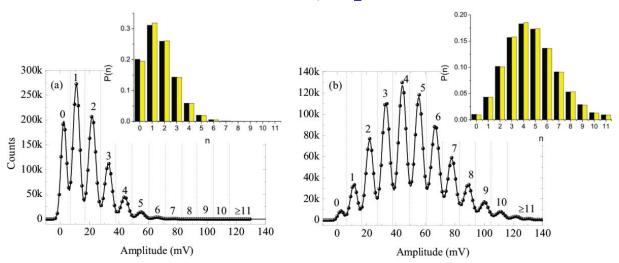


Figure 1. Dots represent the TES counts for two different values of $|\alpha_j\rangle$: each point corresponds to a binning of an amplitude interval of 1.3 mV. Solid lines are the Gaussian fits on the experimental data, while the dotted vertical lines are the thresholds. Part (a) is obtained with a coherent state characterized by a mean photon number per pulse $\mu=31$, while for part (b) the state used had $\mu=87$. The insets of both figures compare the experimental probability distribution (black bars), obtained from measurements binned according to the drawn thresholds, with the corresponding Poisson distributions of mean value $\eta\mu$ (with $\eta=5.1\%$) (yellow bars): as is evident from the plots, the experimental results are in remarkable agreement with the theoretical predictions, showing a fidelity of 99.994 and 99.997%, respectively.

The readout operations on our TES are performed with a dc-SQUID current sensor [39]. Using room-temperature SQUID electronics, we bias our device and read out the current response. Finally, the SQUID output is addressed to a LeCroy 400 MHz oscilloscope, performing the data acquisition, first elaboration and storage. In our experiment, we have illuminated the TES with a power-stabilized fiber-coupled pulsed laser at $\lambda = 1570\,\mathrm{nm}$ (with a pulse duration of 37 ns and a repetition rate of 9 kHz), whose pulse is also used to trigger the data acquisition for a temporal window of 100 ns. The laser pulse energy $(365 \pm 2)\,\mathrm{pJ}$ is measured by a calibrated power meter and then attenuated to the photon-counting regime exploiting two fiber-coupled calibrated attenuators in cascade. The attenuated laser pulses are then sent to the TES detection surface by a single-mode optical fiber. The set of coherent states needed to perform the POVM reconstruction has been generated by lowering the initial laser pulse energy from an initial attenuation of 63.5 dB (corresponding to an average of 130 photons per pulse), to 76.5 dB (mean photon number per pulse: 6.5), to obtain 20 different states $|\alpha_j\rangle = |\sqrt{\tau_j}\alpha\rangle$, where τ_j is the channel transmissivity, $j=1,\ldots,20$.

We work at a fixed wavelength $\lambda=1570$ nm and thus, in ideal conditions, we would expect a discrete energy distribution with outcomes separated by a minimum energy gap $\Delta E=\frac{hc}{\lambda}$. Experimentally, we observe a distribution with several peaks, whose variances represent the energy resolution of the whole detection device. In a first calibration run, after a binning on the oscilloscope channels, we fit the data with a sum of independent Gaussian functions (figure 1

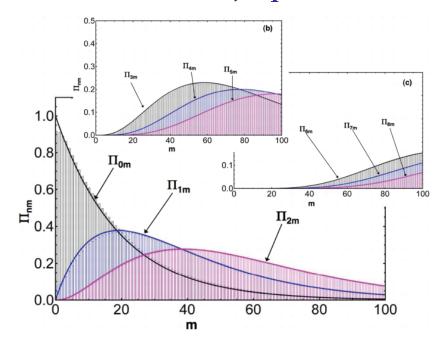


Figure 2. Reconstructed POVM of our TES photon counting systems. Bars represent the matrix elements Π_{nm} as a function of m = 0 and 100 for n = 0, 1, 2 (main plot), n = 3, 4, 5 (b) and n = 6, 7, 8 (c). Continuous lines represent the POVM elements of a linear photon counter with quantum efficiency $\eta = 5.10\%$.

shows that the fitting functions are in excellent agreement with experimental data); the first peak on the left is the '0-peak', corresponding to no photon detection. These fits allowed us to fix the amplitude thresholds (located close to the local minima) corresponding to n detected photons: this way, the histogram of counts is obtained just binning on the intervals identified by these thresholds. The distributions p_{nj} are finally evaluated upon normalizing the histogram bars to the total number of events for the given state⁶. This threshold-based counts binning may introduce some bias or fluctuations since the tails of the nth Gaussian peak fall out of the n counts interval. On the other hand, the effects in neighboring peaks compensate for each other and, overall, do not affect the tomographic reconstruction.

4. Results

The POVM of our TES detection system has been reconstructed up to M = 140 incoming photons and considering N = 12 POVM elements Π_n , n = 0, ..., N - 1, with $\Pi_{N-1} = 1 - \sum_{n=0}^{N-2} \Pi_n$ describing the probability operator for the detection of more than N-2 photons. In figure 2, we show the matrix elements Π_{nm} of the first nine POVM operators (n = 0, ..., 8), for $0 \le m \le 100$. The bars represent the reconstructed Π_{nm} , while the solid lines denote the

⁶ Remarkably, the reconstructions obtained by binning data using thresholds are almost indistinguishable from the ones obtained by evaluating the number of events in the *n*th peak by integrating the corresponding Gaussian of the fit reported in figure 1.

matrix elements of a linear detector. In fact, as mentioned above, the POVM of a linear photon counter can be expressed as a binomial distribution

$$\Pi_n = \sum_{m=n}^{\infty} B_{nm} |m\rangle\langle m| \tag{3}$$

of the ideal photon number spectral measure with $B_{nm} = \binom{m}{n} \eta^n (1-\eta)^{m-n}$, where η is the quantum efficiency of the detector. In order to compare the POVM elements of the linear detector, i.e. B_{nm} , with the reconstructed POVM elements Π_{nm} , we have to first estimate the value of the quantum efficiency η .

This can be done solely on the basis of the experimental data using ML estimation, i.e. we average the values of η which maximize the log-likelihood functions

$$L_{j} = \sum_{n} N_{nj} \log \left(\sum_{m} B_{nm} q_{mj} \right), \tag{4}$$

where N_{nj} is the number of *n*-count events obtained with the *j*th input state $|\sqrt{\tau_j}\alpha\rangle$. The overall procedure leads to an estimated value of the quantum efficiency $\eta = (5.10 \pm 0.04)\%$, where the uncertainty accounts for the statistical fluctuations (for each signal probe we estimated the value of η and then we averaged over the ensemble).

As is apparent from figure 2, we have excellent agreement between the reconstructed POVM and the linear one with the estimated quantum efficiency. In particular, the elements of the POVM are reliably reconstructed for $m \le 100$, whereas for higher values of m the quality of the reconstructions degrades. In the regime $m \le 100$ the fidelity $F_m = \sum_n \sqrt{\prod_{nm} B_{nm}}$ is larger than 0.99 (see the right inset of figure 3), while it degrades to 0.95 for $100 \le m \le 140$. In order to investigate the effects of experimental uncertainties, we performed a sensitivity analysis taking into account the uncertainties on the energy of the input state and on the attenuators, obtaining fidelities always greater than 98.35% for the 12 entries. In order to further confirm the linearity hypothesis, as well as to assess the reliability of the reconstruction, we have compared the measured distributions p_{nj} with those obtained for a linear detector, i.e.

$$l_{nj} = \eta^n \exp(-\eta \mu_j) \mu_j^n / n! \tag{5}$$

and with those obtained using the reconstructed POVM elements, i.e.

$$r_{nj} = \sum_{m=n}^{M} \Pi_{nm} q_{mj}. \tag{6}$$

In figure 3, we report the three distributions for the whole set of probing coherent states, whereas in the left inset we show the (absolute) differences $|p_{nj} - l_{nj}|$ and $|p_{nj} - r_{nj}|$ between those distributions and the measured ones.

As is apparent from the plots, we have excellent agreement between the different determinations of the distributions. This confirms the linear behavior of the detector, and proves that the reconstructed POVM provides a reliable description of the detection process. We have also modified the detection model to take into account the possible presence of dark counts. In this case, upon assuming a Poissonian background, the matrix elements of the POVM are given

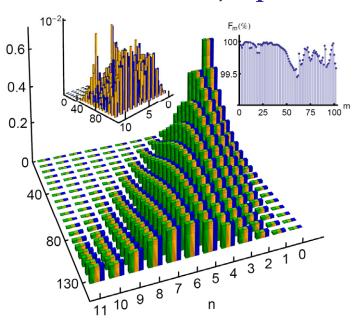


Figure 3. Comparison of the measured distributions p_{nj} (green bars, on the left of each group) of the coherent states $|\alpha_j\rangle$ used for POVM reconstruction with those obtained using the reconstructed POVM elements r_{nj} (yellow central bars) and with those obtained under the linearity hypothesis l_{nj} (blue right bars). The left inset shows the absolute differences $|p_{nj} - r_{nj}|$ (yellow left bars) and $|p_{nj} - l_{nj}|$ (blue right bars). The right inset shows the fidelity F_m between the reconstructed POVM elements at fixed m and those of a linear photon counter with quantum efficiency $\eta = 5.10\%$.

by $\Pi_{nm}=\exp(-\gamma)\sum_{j}\gamma^{j}/j!\,B_{(n-j)m}$ and we have developed an ML procedure to estimate both the quantum efficiency η and the mean number of dark counts per pulse γ . We found that the value of η is statistically indistinguishable from the one obtained with the linear-detector model, whereas the estimated dark counts per pulse are $\gamma=(-0.03\pm0.04)$, in excellent agreement with the direct measurement carried out on our TES detector using the same fitting technique discussed above, providing a substantially negligible dark count level $\gamma=(1.4\pm0.6)\times10^{-6}$. The same conclusion is obtained for any other model, e.g. super-Poissonian, of the background.

In conclusion, we have performed the first tomographic reconstruction of the POVM describing a TES photon detector. Our results clearly validate the description of TES detectors as linear photon counters and, together with the precise estimation of the quantum efficiency, pave the way for practical applications of TES photon counters in quantum technology.

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