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Vertical variations of flux parameters in irradiation channels at the TRIGA Mark II reactor of Pavia

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Abstract

The knowledge of neutron flux parameters, both in terms of value and gradient, in irradiation channels of nuclear reactors is required to avoid biased results when applying Neutron Activation Analysis. To this aim, the Au-Zr bare triple-monitor method with the addition of Lu as a temperature monitor was used to collect experimental data in irradiation channels of three facilities at the TRIGA Mark II reactor of Pavia. Twenty-four monitors were placed in as many positions to determine the vertical variations of the neutron flux parameters. The results obtained in three different activation experiments pointed out a decrease of the conventional fluxes up to 70\% in some cases. Nevertheless, the epithermal neutron flux correction factor, the thermal to epithermal neutron flux ratio and the modified spectral index were constant throughout the entire length of the channels within the core whereas trends were identified in channels outside the core.

Keywords: Neutron flux, Neutron Activation Analysis, TRIGA Mark II reactor

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1. Introduction

The energy distribution of neutrons produced in research nuclear reactors are described by flux parameters depending on the adopted convention. The accurate knowledge of these parameters becomes of fundamental importance when performing Neutron Activation Analysis (NAA) to model the activation of target nuclides in samples.

A number of facilities consisting of one or more vertical channels are usually available for irradiation in a reactor. Although a single channel can accommodate several piled-up samples, flux parameters are not likely to remain constant in space. It was in fact observed, at the 2 MW Interfaculty Reactor Institute in Delft, a significant variation of the investigated flux parameters (several tens of percent with respect to the average value) within a regular, 9 cm length, irradiation container albeit the study highlighted the absence of a defined underlying pattern.[1] Large spread in flux intensity is also expected among channels. As a matter of fact, at the 250 kW TRIGA Mark II reactor of Ljubljana a difference in flux intensity of a factor 7 was estimated between the channel placed at the center of the core and the carousel facility situated outside the core. Moreover, also among the forty irradiation channels of carousel facility, fluctuations in the order of 20% were observed.[2]

Recently, the $k_0$-NAA standardization method was applied at the Radiochemistry and Spectroscopy Laboratory of the Istituto Nazionale di Ricerca Metrologica using the 250 kW TRIGA Mark II nuclear reactor operated by the University of Pavia.[3] The adopted values for the flux parameters were obtained in previous measurements carried out in single positions of different channels. The Cd covered method was used with a set of flux monitors containing Au, Co, Zr and Rb.[4]

In this framework, aiming at reaching the ultimate accuracy in the application of relative- and $k_0$-NAA, we investigated the vertical variation of neutron flux parameters in the irradiation facilities. Significant differences were expected due to the very large length of channels with respect to their diameters.
The bare triple-monitor method\cite{5} with a set of flux monitors containing Au and Zr was adopted to obtain the best position resolution while avoiding the replication of the experiment with and without the Cd cover. In detail, we measured (i) the epithermal neutron flux correction factor, (ii) the thermal to epithermal neutron flux ratio, (iii) the modified spectral index, and (iv) the (conventional) thermal, epithermal and fast fluxes. Additionally, (v) the neutron temperature was measured with Lu monitor in a single point of each irradiation facility.

In the following, after recalling the measurement models used to estimate the flux parameters, we describe the experimental setups and report the results, including the normalized vertical gradients of the thermal and epithermal fluxes.

2. Measurement models

Flux monitors are nuclides converted by neutron capture reactions to radionuclides which are successively quantified through their emitted $\gamma$-rays. Estimates of flux parameters are obtained from the knowledge of the amounts and nuclear parameters of the selected monitors and the outcome of $\gamma$-spectrometry measurements.

Theory and practical aspects regarding the techniques developed to determine flux parameters are described in details in literature.\cite{6} Here we recall the measurement models adopted in this study starting from the basic equations.

The activation of a nuclide detected with $\gamma$-spectrometry is modeled by the following formula:

\begin{equation}
\frac{A_{sp}M}{\theta \Gamma \varepsilon k_{sa} R} = N_A,
\end{equation}

where $A_{sp}$ is the specific $\gamma$-count rate at saturation, $M$ is the molar mass of the target element, $\theta$ is the isotopic abundance of target isotope, $\Gamma$ is the number of emitted gamma rays per disintegration, $\varepsilon$ is the full-energy peak detection efficiency, $k_{sa}$ is the gamma self-absorption correction factor, $R$ is the production rate per target nucleus, and $N_A$ is the Avogadro constant.
Specifically, in case the target nuclide follows a direct activation-decay path,

\[ A_{sp} = \frac{(n_p \lambda_c)}{t_i(1 - e^{-\lambda t})e^{-\lambda t_d}(1 - e^{-\lambda t_c})COI w}, \]  

where \( n_p \) is the net area of the full-energy \( \gamma \)-peak, \( \lambda \) is the decay constant of the activated nuclide, \( t_i \) is the irradiation time, \( t_d \) is the time interval between the end of irradiation and the start of acquisition of \( \gamma \)-spectrum, \( t_c \) and \( t_l \) are the real and live times of the acquired \( \gamma \)-spectrum, \( COI \) is the true-coincidence correction factor for gammas emitted in cascade and \( w \) is the mass of the target element.

In the case of complex activation-decays, different formulae are available to calculate \( A_{sp} \). For example, when the analytically interesting radionuclide is the daughter, II, of the directly formed one, I, the following equation applies:

\[ A_{sp} = \frac{n_{p,II} t_c}{t_l w} \frac{\lambda_{II} - \lambda_I}{\lambda_I \lambda_{I}^{-1} S_I D_I C_I - \lambda_I \lambda_{II}^{-1} S_{II} D_{II} C_{II}}, \]  

where \( S, D \) and \( C \) are \( 1 - e^{-\lambda t_i}, e^{-\lambda t_d} \) and \( 1 - e^{-\lambda t_c} \), respectively, and subscripts I and II refer to the produced radionuclides.

In addition, \( R = G_s \Phi_{th} \sigma_0 + G_e \Phi_e I_0(\alpha) \) if the Hogdahl convention is adopted for nuclides with \( 1/v \) neutron capture cross section\(^[6] \), or \( R = n v_0 \sigma_0 (G_{th} g(T_n) + G_r r(\alpha) \sqrt{\frac{T_n}{T_0}} s_0(\alpha)) \) when the modified Westcott formalism is exploited instead for nuclides that do not follow the \( 1/v \) behavior\(^[7] \). Among the parameters in \( R \) definitions, \( G_s \) is the (Hogdahl) thermal (sub-cadmium) neutron self-shielding factor, \( \Phi_{th} \) is the conventional thermal neutron flux, \( \sigma_0 \) is the \( (n,\gamma) \) reaction cross section at 2200 m s\(^{-1} \) neutron velocity, \( v_0 \), \( G_e \) is the (Hogdahl) epithermal (epi-cadmium) neutron self-shielding factor, \( \Phi_e \) is the conventional epithermal neutron flux, \( \alpha \) is the epithermal neutron flux correction factor, \( I_0(\alpha) \) is the resonance integral for a \( 1/E^{1+\alpha} \) epithermal flux, \( n \) is the total neutron density, \( G_{th} \) is the (Westcott) thermal neutron self-shielding factor, \( g(T_n) \) is the Westcott factor at the neutron temperature \( T_n \), \( G_r \) is the resonance neutron self-shielding, \( r(\alpha) \sqrt{\frac{T_n}{T_0}} \) is the modified spectral index, which includes the epithermal to total
neutron density ratio, and \( s_0(\alpha) \) is the resonance to thermal \((n,\gamma)\) cross section ratio.

### 2.1. Bare triple-monitor method

The bare triple-monitor method is based on the use of three monitors. The combination of Eq. (1) multiplied by \( \frac{\theta_{Au} \Gamma_{Au} \sigma_{Au}}{M_{Au}} \) and applied to monitors 1 and 2 provides the following formula:

\[
\frac{A_{sp,1} \sigma_0}{k_{0,Au}(1) \varepsilon_1 k_{sa,1} R_1} = \frac{A_{sp,2} \sigma_0}{k_{0,Au}(2) \varepsilon_2 k_{sa,2} R_2},
\]

where subscripts 1 and 2 refer to the two monitors and \( k_{0,Au}(i) = \frac{\theta_i \Gamma_i \sigma_i}{\theta_{Au} \Gamma_{Au} \sigma_{Au} M_{Au}} \) is a composite nuclear standardization factor referred to an element \( i \) with respect to the Au standard.\(^6\)

In the case of Hogdahl convention and under the assumption that \( \Phi_{th,1} = \Phi_{th,2} \) and \( \Phi_{e,1} = \Phi_{e,2} \), i.e. the monitors are exposed to the same flux, Eq. (4) can be rearranged to obtain the conventional thermal to epithermal flux ratio:

\[
f = \frac{k_{0,Au}(1) \varepsilon_1 G_{e,1} Q_{0,1}(\alpha) - A_{sp,1} k_{sa,2} G_{e,2} Q_{0,2}(\alpha)}{G_{e} \left( A_{sp,1} k_{sa,2} - \frac{k_{0,Au}(1) \varepsilon_1}{k_{0,Au}(2) \varepsilon_2} \right)},
\]

where \( Q_{0}(\alpha) = \frac{I_0(\alpha)}{\sigma_0} = \frac{Q_0}{E_0} - 0.429 \left( \frac{E}{E_0} \right)^{2(\alpha + 1)/0.55} \); \( Q_0 \) is the resonance integral to \( \sigma_0 \) for a 1/E epithermal flux and \( E_0 \) is the effective resonance energy that is considered independent from \( \alpha \).\(^8\)

In the case of Westcott convention and under the assumption that the monitors are exposed to the same thermal and epithermal neutron densities, from Eq. (4) it derives the so called modified spectral index:

\[
r(\alpha) \sqrt{\frac{T_n}{T_0}} = \frac{G_{th} \left( A_{sp,1} k_{sa,2} g_2(T_n) - \frac{k_{0,Au}(1) \varepsilon_1}{k_{0,Au}(2) \varepsilon_2} g_1(T_n) \right)}{G_{r,1} s_0,1(\alpha) - A_{sp,1} k_{sa,2} G_{r,2} s_0,2(\alpha)},
\]

It is worth to note that the knowledge of \( \alpha \) is required to compute \( f \) and \( r(\alpha) \sqrt{\frac{T_n}{T_0}} \). The use of three 1/v monitors is suitable to estimate \( \alpha \) by com-
Combining Eq. (5) applied to monitors 1 and 2 and to monitors 1 and 3, rearranged to obtain the following equation:

\[
\left( \frac{1}{A_{sp,1,k_{sa,1,k_{0,Au}(2)}\varepsilon_2}} - 1 \right) - \left( \frac{1}{A_{sp,2,k_{sa,1,k_{0,Au}(1)}\varepsilon_1}} - 1 \right) \times G_{e,1}Q_{0,1}(\alpha) - \left( \frac{1}{A_{sp,3,k_{sa,1,k_{0,Au}(1)}\varepsilon_1}} - 1 \right) \times G_{e,2}Q_{0,2}(\alpha) + \left( \frac{1}{A_{sp,3,k_{sa,1,k_{0,Au}(1)}\varepsilon_1}} - 1 \right) \times G_{e,3}Q_{0,3}(\alpha) = 0, \\
\]

(7)

where subscripts 1, 2, 3 refer to the three monitors. The \( \alpha \) value is obtained numerically as the implicit solution of Eq. (7).

There is a combination of monitors providing the practically attainable lowest uncertainty for the determination of \( \alpha \). Specifically, the three monitors should have the largest possible spread in the \( \overline{E}_r \) and \( Q_0 \) values. Among the different monitor data sets developed and tested, the most used consists of \(^{197}\text{Au},^{94}\text{Zr}\) and \(^{96}\text{Zr}\) and the adopted neutron capture reactions are \(^{197}\text{Au}(n,\gamma)^{198}\text{Au},^{94}\text{Zr}(n,\gamma)^{95}\text{Zr}\) and \(^{96}\text{Zr}(n,\gamma,\beta^{-})^{97m}\text{Nb}\). This combination gives practical advantages because \( \text{Zr} \) provides two monitors reflecting in a simpler sample preparation; in addition, as the adopted gammas are not emitted in cascade, they are not affected by true-coincidences (COI = 1).

2.2. Conventional thermal, epithermal and fission neutron fluxes

The conventional thermal and epithermal neutron fluxes are computed from the following equations applied to one of the three monitors and obtained by rearranging Eq. (1):

\[
\Phi_{th} = \frac{A_{sp}M}{\theta \Gamma \varepsilon_{k_{sa}} N_A \sigma_0 \left( G_s + G_c Q_0(\alpha) \right)}, \\
\]

(8)

\[
\Phi_{e} = \frac{A_{sp}M}{\theta \Gamma \varepsilon_{k_{sa}} N_A \sigma_0 \left( G_s f + G_c Q_0(\alpha) \right)}. \\
\]

(9)
The fission component can be retrieved using monitor sets containing a nuclide activated through fast neutrons. Among the available nuclides, a convenient choice is the $^{90}$Zr via the reaction $^{90}$Zr(n,2n)$^{89}$Zr. In this case the reaction rate per target nucleus is due to the fission component, i.e. $R = \Phi f \sigma_f$, where $\Phi_f$ is the conventional fission flux and $\sigma_f$ is the $^{235}$U spectrum averaged cross section for the reaction $^{90}$Zr(n,2n)$^{89}$Zr.

From Eq.(1) it follows:

$$\Phi_f = \frac{A_{sp}M}{\theta \Gamma \epsilon_k N_A \sigma_f}.$$  \hfill (10)

### 2.3. Neutron temperature

A further monitor added to the bare triple-monitor allows the measurement of the neutron temperature. For this purpose, Lu is generally adopted via the reaction $^{176}$Lu(n,$\gamma$)$^{177}$Lu. Since the isotope $^{176}$Lu is a non $1/v$ nuclide, $g_{\text{Lu}}(T_n)$ deviates from unity according to $T_n$.\[9\]

The $g_{\text{Lu}}(T_n)$ value is obtained from Eq.(6) applied to Lu and one of the available $1/v$ monitors, say monitor 1. Accordingly,

$$g_{\text{Lu}}(T_n) = \frac{1}{G_{\text{th},\text{Lu}}} \left( \frac{A_{sp,\text{Lu}} k_{0,\text{Au}}(1) \epsilon_{1,\text{sa,1}}}{A_{sp,1} k_{0,\text{Au}}(\text{Lu}) \epsilon_{\text{Lu,sa,Lu}}} \times \left( G_{\text{th,1}} g_1(T_n) + G_{r,1} r(\alpha) \sqrt{\frac{T_n}{T_0}} s_{0,1}(\alpha) \right) ight) - G_{r,\text{Lu}} r(\alpha) \sqrt{\frac{T_n}{T_0}} s_{0,\text{Lu}}(\alpha),$$  \hfill (11)

where subscripts Lu and 1 refer to Lu and the monitor used as comparator, respectively. It is worth noting that as monitor 1 follows $1/v$ behavior, $g_1(T_n) \cong 1$. The $s_0(\alpha)$ value can be obtained from $s_0(\alpha) = \frac{s_0}{E_0^2}$,\[11\] where $s_0$ is available in literature for non $1/v$ monitors while it can be computed from $s_0 = \frac{2}{\sqrt{\pi}} (Q_0 - 0.429)$ for $1/v$ monitors. The $T_n$ value is finally estimated from the measured $g_{\text{Lu}}(T_n)$ using the (known) function linking $g_{\text{Lu}}(T_n)$ to $T_n$.\[11\]
3. Experimental

3.1. Irradiation facilities

The TRIGA Mark II working in Pavia is a 250 kW pool-type research reactor fueled with low-enriched $^{235}\text{U}$ and moderated with demineralized light water. At present, the reactor operates weekly from Monday to Friday for about 30 h non-continuously.

The core is composed by ninety slots occupied by fuel elements, neutron sources and three control rods (SHIM, REG and TRANS) placed in five concentric rings around a central channel, 40 cm useful length and 26 mm diameter, used as irradiation facility and called Central Channel, CC. One of the slots of the outer ring houses a channel, 10 cm useful length and 15 mm diameter, used as a short time irradiation facility and called Rabbit, RB. Additional forty channels, 27 cm useful length and 26 mm diameter, coded from 1 to 40 and located in a carousel inside a graphite reflector surrounding the core, are available in an irradiation facility called Lazy Susan, LS. Samples are manually inserted in the irradiation channels with the exception of the Rabbit facility, where a pneumatic system is available for users. The position of the irradiation facilities is shown in the schematic horizontal cross section of the reactor displayed in Fig.1.

3.2. Preparation and neutron exposure of monitor samples

In this study we measured the neutron flux parameters using 24 monitor samples distributed in as many irradiation positions. Specifically, 10 samples were located in CC, 5 in RB, 3 in LS-26, and 6 in LS-27.

Each monitor sample was prepared by weighing 30 µL volume of a mono-elemental Au solution pipetted on a 6 mm diameter filter paper disk placed in a 1 mL polyethylene (PE) vial. In a few cases, 30 µL volume of a mono-elemental Lu solution was added to probe the neutron temperature. After drying with an infrared lamp, a 6 mm diameter disk of pure Zr was pressed on the filter paper disk. The vial was finally heat-sealed to avoid vertical displacements. A sketch of the monitor sample in its 1 mL vial is zoomed in Fig.2.
Specifically, two solutions, $S_{Au1}$ and $S_{Au2}$, were prepared by dilution 1:15 and 1:6 of a SI traceable 1000 µg mL$^{-1}$ Au standard solution, Sigma-Aldrich. $S_{Au1}$ was used for monitors in CC and RB, $S_{Au2}$ was used for monitors in LS. In the case of monitor samples including Lu, an SI traceable 1000 µg mL$^{-1}$ Lu standard solution, Sigma-Aldrich, was used. Disks of Zr, 99.2% purity, 0.1 mm and 0.5 mm thickness, GoodFellow, were used; the thin ones in CC and RB, and the thick ones in LS.

The masses of the pipetted solutions and disks were measured using a SI traceable analytical balance.
It is worth to note that total thickness of the stacked filter paper and Zr disk was kept lower than 1 mm. This assured a good spatial resolution of the measurement and a negligible vertical variation of the probed neutron flux.

The vials were fixed in equally spaced vertical positions at the center axis of PE irradiation containers using PE inserts. The monitor samples used in CC, RB and LS were distributed in 3, 1 and 3 containers, respectively, and sent to irradiation. The layouts of monitors in the containers placed in the different facilities are shown in Fig. 2. The vertical distance, $d$, of each monitor with respect to the bottom of the piled-up containers is indicated.

![Figure 2: Layouts of the containers placed in the channels of the different irradiation facilities. The vertical position, $d$, of each monitor sample with respect to the bottom of the channel is showed. The asterisks indicate the monitors including Lu for neutron temperature measurements. The height of the 1 mL vial and the position of the monitor sample are shown in the zoom. Distances are in cm.](image)

Three irradiations lasting 3600 s were sequentially performed with the reactor at 250 kW critical power. The first one was carried out in CC by introducing the containers with the reactor powered-off, whereas the second and the third
ones in RB and LS with the reactor powered-on. The carousel of LS facility was not rotating during the irradiation.

During irradiation, the TRANS control rod was completely extracted and the SHIM was fixed in a vertical position selected to maintain the critical power with the REG moving close to the equator of the core.

Sinusoidal displacements of REG around the central position were negligible. In addition, the vertical position of the REG was similar in the three irradiations.

This is the typical layout of the control rods adopted when samples are irradiated for NAA to limit the variability of neutron flux parameters due to different arrangements of the control rods.\[13\]

3.3. Gamma spectrometry measurements

The 1 mL vials holding the monitors were extracted from the irradiation containers after about 16 h cooling time and fixed at the center of plastic circular containers for $\gamma$-counting. The $\gamma$-spectrometry measurements were carried out using a CANBERRA GC3518 HPGe detector (35% relative efficiency, 1.96 keV FWHM at 1332.5 keV energy) connected to an ORTEC DSPEC 502 multi-channel analyzer. Samples were manually placed at 10 cm distance from the end-cap of the GC3518 by means of a plastic spacer; this quite large distance was chosen to limit the effect of sample positioning. The detection system was calibrated in energy and efficiency using a certified multi-$\gamma$ source.

Each monitor sample was counted twice. A first (short) acquisition, lasting about 1 h, was performed within 24 h after the irradiation end to quantify the 411.8 keV $^{198}$Au, the 743.4 keV $^{97m}$Nb and, if present, the 208.4 keV $^{177}$Lu $\gamma$-peaks. After 2 or 3 days, a second (long) acquisition, lasting about 24 h, was performed to quantify the 756.7 keV $^{95}$Zr and 909.2 keV $^{89}$Zr $\gamma$-peaks. Acquisition times were online adjusted to determine the net area of the $\gamma$-peaks with a relative uncertainty due to counting statistics lower than 0.2%. During data collection, the pile-up rejection circuit was active and the recorded relative dead time was always below 10%. 

11
4. Results and discussion

The forty-eight collected γ-spectra were processed using the moderate count rate and regular peaks algorithm of the HyperLab software to calculate the net area of the γ-peaks. The corresponding specific γ-count rates at saturation of $^{198}$Au, $^{95}$Zr, $^{89}$Zr and $^{177}$Lu were computed via Eq.(2) whereas Eq.(3) was used for $^{97m}$Nb.

First, $\alpha$ was obtained by solving Eq.(7) with $^{197}$Au, $^{94}$Zr and $^{96}$Zr as monitor 1, 2 and 3, respectively. The resulting $\alpha$ value was used to compute $f$ and $r(\alpha)\sqrt{\frac{T_n}{T_0}}$ according to Eq.(5) and (6), respectively. The corresponding (Hogdahl) conventional fluxes $\Phi_{th}$, $\Phi_e$ and $\Phi_f$ were calculated via Eq.(8), (9) and (10), respectively, using the $^{197}$Au monitor. The $^{197}$Au was also adopted as monitor 1 in Eq.(11) for the measurement of the neutron temperature.

The $k_0$, $\sigma_0$, $Q_0$, $s_0$, $E_r$ and $\lambda$ values, including their uncertainty, were retrieved from the $k_0$ database[14] while for $\sigma_f$ the most up to date literature value was adopted.[15] The $Q_{0,Au}$ value was converted to $s_{0,Au}$ in order to apply Westcott formalism in Eq.(11). The $M_{Au}$, $\theta_{Au}$, $\Gamma_{Au}$ and $N_A$ values adopted in Eq.(8), (9) and (10) were retrieved from literature.[16, 17, 18]

The effect of γ-rays self-absorption was neglected for Au and Lu pipetted on the filter paper while it was evaluated for Zr disks by taking into account thickness and linear attenuation coefficient at given γ-energies.[19] The resulting influence was negligible with the exception of the 0.5 mm thickness for which the $k_{sa}$ correction factor was close to 0.99.

Thermal, sub-cadmium, epithermal and resonance self-shielding factors, $G_{th}$, $G_s$, $G_e$ and $G_r$ were assumed equal to unity with the exception of $G_e$ for the $^{94}$Zr and $^{96}$Zr, calculated with the polynomial fit proposed by De Corte.[6]

The Westcott $g_{Au}(T_n)$ factor in Eq.(11) was also considered equal to the unity under the reasonable assumption that the Au cross section function follows a perfect $1/v$ behavior until 2 eV energy.

The above reported formulae were implemented in a Microsoft Excel spreadsheet to calculate $\alpha$, $f$, $r(\alpha)\sqrt{\frac{T_n}{T_0}}$, $\Phi_{th}$, $\Phi_e$, $\Phi_f$ and $T_n$, including their combined
uncertainties evaluated by means of the sensitivity coefficient method. The main contributors to the evaluated uncertainties are shown in Table 1.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>1st contributor</th>
<th>2nd contributor</th>
<th>3rd contributor</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \alpha / 1 )</td>
<td>( \varepsilon )</td>
<td>( k_{0,\text{Au}}(^{94}\text{Zr}) )</td>
<td>( Q_{0,\text{Au}} )</td>
</tr>
<tr>
<td>( f / 1 )</td>
<td>( \alpha )</td>
<td>( k_{0,\text{Au}}(^{94}\text{Zr}) )</td>
<td>( Q_{0,\text{96Zr}} )</td>
</tr>
<tr>
<td>( r(\alpha)\sqrt{\frac{T_n}{T_0}} / 1 )</td>
<td>( \alpha )</td>
<td>( k_{0,\text{Au}}(^{94}\text{Zr}) )</td>
<td>( s_{0,\text{96Zr}} )</td>
</tr>
<tr>
<td>( \Phi_{th} / \text{cm}^{-2}\text{s}^{-1} )</td>
<td>( f )</td>
<td>( \varepsilon )</td>
<td>( Q_{0,\text{Au}} / \alpha )</td>
</tr>
<tr>
<td>( \Phi_f / \text{cm}^{-2}\text{s}^{-1} )</td>
<td>( f )</td>
<td>( \varepsilon )</td>
<td>( Q_{0,\text{Au}} / \alpha )</td>
</tr>
<tr>
<td>( \sigma_f / \text{cm}^{-2}\text{s}^{-1} )</td>
<td>( \sigma_f )</td>
<td>( \eta_f )</td>
<td>( \theta )</td>
</tr>
<tr>
<td>( g_{\text{Lu}}(T_n) / 1 )</td>
<td>( k_{0,\text{Au}}(\text{Lu}) )</td>
<td>( r(\alpha)\sqrt{\frac{T_n}{T_0}} )</td>
<td>( s_{0,\text{Au}} )</td>
</tr>
<tr>
<td>( T_n / ^\circ\text{C} )</td>
<td>( g_{\text{Lu}}(T_n) )</td>
<td>-</td>
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</tr>
</tbody>
</table>

Table 1: Main contributors to the combined uncertainty for the measured flux parameters in CC, RB and LS ranked in descending order of importance.

The \( \alpha \) and \( f \) values measured in CC, RB and LS-27 versus the distance \( d \) are plotted in Fig.3. In addition, the \( r(\alpha)\sqrt{\frac{T_n}{T_0}} \) values are shown in Fig.A.1 of the Appendix.

The measured \( \alpha \), \( f \) and \( r(\alpha)\sqrt{\frac{T_n}{T_0}} \) values in CC and RB did not show significant trends. Specifically, the \( \alpha \) scattering was in agreement with the calculated \( \alpha \) averages \(-0.0347(91)\) and \(-0.0356(92)\) in CC and RB, respectively. A similar agreement was observed for the \( f \) data with the averages \( 19.2(10) \) and \( 19.6(10) \) in CC and RB, respectively, and for the \( r(\alpha)\sqrt{\frac{T_n}{T_0}} \) data with the averages \( 0.0450(20) \) and \( 0.0442(20) \) in CC and RB, respectively. Here and hereafter, the uncertainties \((k = 1)\) in parentheses apply to the last respective digits. The mean of the single evaluated uncertainties was assigned to the calculated average.

Significant linear trends were identified in LS-27; in addition, the agreement between the values recorded in LS-26 and LS-27 confirmed the trends and pointed out the absence of appreciable differences. The data obtained in LS-27 were fitted by a straight line \( y = bd + c \) to quantify the slope, \( b \), and the intercept, \( c \), for \( \alpha \), \( f \) and \( r(\alpha)\sqrt{\frac{T_n}{T_0}} \). The \( b \) and \( c \) fitting parameters are reported in Table 2 together with the uncertainty, \( u(y) \), of the value obtained when using the model \( y \). The mean of the single evaluated uncertainties was assigned to
Figure 3: The $\alpha$ and $f$ values measured in CC, RB and LS-27 at different vertical distance, $d$, with respect to the bottom of the stacked irradiation container. Error bars indicate the expanded ($k=2$) uncertainties. Averages and straight lines fitting the data are displayed.

$u(y)$.

The $\Phi_{th}$ and $\Phi_e$ values measured in CC, RB and LS-27 versus the distance $d$ are plotted in Fig. 4. In addition, the $\Phi_t$ values are shown in Fig. A.1 of the Appendix.

Significant trends of the measured $\Phi_{th}$, $\Phi_e$ and $\Phi_t$ values were identified in CC, RB and LS-27; the trends in LS-27 and the absence of appreciable differences with its adjacent channel were confirmed and pointed out by the results obtained with the 3 monitor samples located in LS-26. The data were fitted by a parabola $y = ad^2 + bd + c$ with the exception of the $\Phi_e$ and $\Phi_t$ values in LS-27 which were fitted by a straight line $y = bd + c$.

The $a$, $b$ and $c$ fitting parameters are reported in Table 3 together with the
Table 2: Computed values for slope, $b$, and intercept, $c$, of the straight line $y = bd + c$ fitting the $\alpha$, $f$ and $r(\alpha)\sqrt{T_n}$ values measured in LS-27. The fitting uncertainties ($k = 1$) in parentheses apply to the last respective digits. The uncertainty associated to $y$, $u(y)$, is given.

<table>
<thead>
<tr>
<th>Channel</th>
<th>Parameter / cm$^{-1}$</th>
<th>$b / \text{cm}^{-1}$</th>
<th>$c / 1$</th>
<th>$u(y) / 1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>LS-27</td>
<td>$\alpha$</td>
<td>6.4(14)$\times 10^{-4}$</td>
<td>-0.0101(16)</td>
<td>0.010</td>
</tr>
</tbody>
</table>

relative uncertainty, $u_r(y)$, of the value obtained when using the model $y$. The mean of the single evaluated relative uncertainties was assigned to $u_r(y)$.

<table>
<thead>
<tr>
<th>Channel</th>
<th>Parameter / cm$^{-2}$s$^{-1}$</th>
<th>$a / \text{cm}^{-4}$s$^{-1}$</th>
<th>$b / \text{cm}^{-3}$s$^{-1}$</th>
<th>$c / \text{cm}^{-2}$s$^{-1}$</th>
<th>$u_r(y) / 1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CC</td>
<td>$\Phi_{th}$</td>
<td>-1.111(40)$\times 10^{10}$</td>
<td>3.35(15)$\times 10^{11}$</td>
<td>4.17(11)$\times 10^{12}$</td>
<td>3.3%</td>
</tr>
<tr>
<td></td>
<td>$\Phi_e$</td>
<td>-6.25(31)$\times 10^{8}$</td>
<td>1.95(11)$\times 10^{10}$</td>
<td>2.005(89)$\times 10^{11}$</td>
<td>3.7%</td>
</tr>
<tr>
<td></td>
<td>$\Phi_f$</td>
<td>-8.11(89)$\times 10^{9}$</td>
<td>2.48(33)$\times 10^{11}$</td>
<td>2.58(25)$\times 10^{12}$</td>
<td>5.7%</td>
</tr>
<tr>
<td>RB</td>
<td>$\Phi_{th}$</td>
<td>-7.6(10)$\times 10^9$</td>
<td>2.3(19)$\times 10^{10}$</td>
<td>3.043(40)$\times 10^{11}$</td>
<td>3.4%</td>
</tr>
<tr>
<td></td>
<td>$\Phi_e$</td>
<td>-3.35(34)$\times 10^8$</td>
<td>7.7(35)$\times 10^{8}$</td>
<td>1.5540(76)$\times 10^{11}$</td>
<td>3.7%</td>
</tr>
<tr>
<td></td>
<td>$\Phi_f$</td>
<td>-1.02(50)$\times 10^{10}$</td>
<td>8.5(53)$\times 10^{10}$</td>
<td>1.37(11)$\times 10^{12}$</td>
<td>5.2%</td>
</tr>
<tr>
<td>LS-27</td>
<td>$\Phi_{th}$</td>
<td>-8.3(38)$\times 10^8$</td>
<td>-8.5(88)$\times 10^9$</td>
<td>1.219(36)$\times 10^{12}$</td>
<td>3.4%</td>
</tr>
<tr>
<td></td>
<td>$\Phi_e$</td>
<td>-1.704(72)$\times 10^9$</td>
<td>5.980(82)$\times 10^{10}$</td>
<td>3.7%</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\Phi_f$</td>
<td>-5.53(27)$\times 10^9$</td>
<td>2.053(30)$\times 10^{11}$</td>
<td>6.1%</td>
<td></td>
</tr>
</tbody>
</table>

Table 3: Computed values for $a$, $b$ and $c$ of the parabola $y = ad^2 + bd + c$ fitting the $\Phi_{th}$, $\Phi_e$ and $\Phi_f$ data measured in CC, RB and LS. The fitting uncertainties ($k = 1$) in parentheses apply to the last respective digits. The relative uncertainty associated to $y$, $u_r(y)$, is given.

A quantitative information on the effect of the local deviations can be pointed out by the normalized gradient of the conventional flux, $v(\Phi) = \frac{1}{\Phi} \frac{\partial \Phi}{\partial d}$. The results based on parabolas and straight lines fitting $\Phi_{th}$ and $\Phi_e$ in CC, RB and LS are plotted in Fig. 5.

The $g_{lu}(T_n)$ values in CC, RB and LS-27 resulted to be 1.94(11), 1.84(11) and 1.85(11), respectively, corresponding to $54(16)$ °C, $35(15)$ °C and $40(15)$ °C neutron temperatures. Quoted uncertainties were due to the uncertainties of $g_{lu}(T_n)$ amplified by the function linking $g_{lu}(T_n)$ to $T_n$.

To sum up, the data pointed out that $\alpha$ was close to $-0.035$ both along the 40 cm length channel of CC and along the 10 cm length channel of RB whereas it showed a (small) positive trend across 0.00 along the 27 cm length channel.
Figure 4: The $\Phi_h$ and $\Phi_e$ values measured in CC, RB and LS-27 at different vertical distance, $d$, with respect to the bottom of the stacked irradiation container. Error bars indicate the expanded ($k = 2$) uncertainties. Parabolas or straight lines fitting the data are displayed. The left side ordinate axis indicates the absolute value while the right side indicates the conventional flux normalized to the vertex of the parabola or to the intercept of the straight line.

of LS-27. Similarly, $f$ was close to 20 both in CC and RB whereas it showed a (major) positive trend starting from 20 up to 30 in LS-27. In addition, $r(\alpha)\sqrt{\frac{T_n}{T_0}}$ was close to 0.045 both in CC and RB whereas it showed a (major) negative trend starting from 0.040 up to 0.030 in LS-27.

Concerning the conventional fluxes, a noteworthy decrease of $\Phi_h$ and $\Phi_e$ up to 60% was observed in CC with respect to the $6.69(22) \times 10^{12} \text{cm}^{-2} \text{s}^{-1}$ and $3.53(12) \times 10^{11} \text{cm}^{-2} \text{s}^{-1}$ maximum, respectively, occurring at 15 cm distance from the bottom of the channel. A reduction of $\Phi_f$ up to 70% was detected with respect to the $4.47(27) \times 10^{12} \text{cm}^{-2} \text{s}^{-1}$ maximum occurring at the same 15 cm
Figure 5: The normalized flux gradients, $v(\Phi_{th})$ and $v(\Phi_e)$, in CC, RB and LS-27 at different vertical distance, $d$, with respect to the bottom of the stacked irradiation container. Vertical dashed lines show the position where the first derivative of the flux is zero.

distance.

A minor but still significant decrease of $\Phi_{th}$ and $\Phi_e$ up to 20% was observed in RB with respect to the $3.06(10) \times 10^{12} \text{ cm}^{-2} \text{s}^{-1}$ and $1.56(8) \times 10^{11} \text{ cm}^{-2} \text{s}^{-1}$ maximum, respectively, occurring at 1.5 cm. A reduction of $\Phi_t$ up to 20% was detected with respect to the $1.55(8) \times 10^{12} \text{ cm}^{-2} \text{s}^{-1}$ maximum occurring at 4 cm.

In LS-27, the results pointed out a remarkable decrease up to 50% of $\Phi_{th}$ and up to 60% of $\Phi_e$ with respect to the $1.24(4) \times 10^{12} \text{ cm}^{-2} \text{s}^{-1}$ and $5.98(23) \times 10^{10} \text{ cm}^{-2} \text{s}^{-1}$ maximum, respectively, starting from the channel bottom. A reduction of $\Phi_t$ up to 60% was detected with respect to the $2.05(12) \times 10^{11} \text{ cm}^{-2} \text{s}^{-1}$ maximum at the channel bottom.
The data collected in this study can be compared with the literature results reported in Table 4. Specifically, the $\alpha$ value measured in CC, RB and LS published in 2017[4] is in agreement, the $f$ value is lower while the $\Phi_{th}$ and $\Phi_e$ values are within the variability range observed along the channels. Likewise, the $f$ value measured in CC, RB and LS published in 2014[20] is lower whereas the $\Phi_{th}$ and $\Phi_e$ values are within and outside, respectively, the observed variability range.

<table>
<thead>
<tr>
<th></th>
<th>CC</th>
<th>RB</th>
<th>LS</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Phi_{th}$ / cm$^{-2}$s$^{-1}$</td>
<td>6.11(16)$\times10^{12}$</td>
<td>2.54(7)$\times10^{12}$</td>
<td>1.02(3)$\times10^{12}$</td>
</tr>
<tr>
<td>$\Phi_e$ / cm$^{-2}$s$^{-1}$</td>
<td>3.92(6)$\times10^{11}$</td>
<td>1.62(3)$\times10^{11}$</td>
<td>5.88(9)$\times10^{10}$</td>
</tr>
<tr>
<td>$\alpha$ / 1</td>
<td>-0.036(6)</td>
<td>-0.041(7)</td>
<td>-0.016(6)</td>
</tr>
<tr>
<td>$f$ / 1</td>
<td>15.6(3)</td>
<td>15.7(4)</td>
<td>17.4(4)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>CC</th>
<th>RB</th>
<th>LS</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Phi_{th}$ / cm$^{-2}$s$^{-1}$</td>
<td>6.84$\times10^{12}$</td>
<td>3.04$\times10^{12}$</td>
<td>1.13$\times10^{12}$</td>
</tr>
<tr>
<td>$\Phi_e$ / cm$^{-2}$s$^{-1}$</td>
<td>4.26$\times10^{11}$</td>
<td>1.90$\times10^{11}$</td>
<td>7.93$\times10^{10}$</td>
</tr>
<tr>
<td>$\alpha$ / 1</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>$f$ / 1</td>
<td>16.1</td>
<td>16.0</td>
<td>14.2</td>
</tr>
</tbody>
</table>

Table 4: Neutron flux parameters measured in previous experiments in CC, RB and LS. (*) Values obtained after conversion of the published integral flux data.

5. Conclusion

The knowledge of the variation of neutron flux parameters is a precondition to reach the ultimate accuracy when performing NAA in a reactor.

To this aim, vertical deviations of $\alpha$, $f$, modified spectral index and conventional thermal, epithermal, fast fluxes were measured in the CC, RB and LS irradiation facilities of the TRIGA Mark II reactor of Pavia. Neutron temperature was also probed in single positions.

The reproducibility of the results allowed observing the profile of neutron flux parameters along the channels. Specifically, the conventional fluxes strongly decreased up to tens of percent in few centimeters when moving from the maximum in all the facilities. Nevertheless, no variations of $f$, modified spectral
index and $\alpha$ were detected in CC and RB while significant trends were identified in LS. In addition, the neutron temperature was higher in CC with respect to RB and LS.

Constant $\alpha$ and $f$ values significantly simplify the NAA measurement equation only if the thermal and epithermal fluxes are constant too. The data collected in this study pointed out that the assumption of constant thermal and epithermal fluxes does not hold in a TRIGA Mark II reactor with the exception of samples vertically piled-up in a few mm and located in selected positions of CC and RB. In the remaining cases, e.g. when a large number or voluminous samples are simultaneously analyzed or the LS facility is used, monitors for $k_0$-NAA (or standards for relative-NAA) should surround the samples to receive the same flux. As an alternative, the effect of neutron flux parameters variations can be corrected taking into account the actual irradiation position of samples and monitors and using model functions calculated with previous data.

It is worth to note that the fast flux measured in LS was less than one twentieth of the fast flux measured in CC although the $f$ at the bottom was (unexpectedly) close to the value measured in CC and RB. Since both the Hogdahl and the Westcott conventions do not consider the fast flux region, best results are obtained with $k_0$-NAA when the fast flux is negligible with respect to the thermal and epithermal fluxes. Moreover, threshold reactions produce interfering radionuclides that should be corrected both in relative- and $k_0$-NAA.

The knowledge of the regular trends observed in the TRIGA Mark II reactor of Pavia is useful to properly place samples, monitors and standards in order to limit the effect of gradients. In this context, the measurement of flux parameters should be repeated at fixed intervals or in case of rearrangement of the reactor core to check the time stability of the values.

6. Acknowledgment

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Appendix A.

Figure A.1: The $r(\alpha)\sqrt{\frac{T}{n}}$ and $\Phi_f$ values measured in CC, RB and LS-27. Expanded uncertainties are reported with coverage factor $k = 2$. The solid lines display the averages, parabola or straight lines fitting the data.
References


[8] J. op de Beeck, Critical evaluation of the effective resonance energy concept and the epithermal neutron spectrum shape-factor $\alpha$ for reac-


[14] $k_0$ database

URL http://www.kayzero.com/k0nnaa/k0nnaaorg/Nuclear_Data_SC/Entries/2016/1/11_New_k0-data_Library_2015.html


